

The background of the entire page is a deep space image featuring a starry field and a nebula. A horizontal teal band is overlaid across the middle of the image. The word 'RAD' is centered in this band in a large, bold, black font. Below it, the text 'Summer Project 2021' and 'Astronomy Club IITK' is centered in a smaller, black font.

# RAD

Summer Project 2021

Astronomy Club IITK

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Several aspects of the handbook have been adapted from the following two books and we sincerely owe the authors of these books for writing such excellent guides to budding astrophysicists:

- *An Introduction to Modern Astrophysics* by Bradley W. Carroll and Dale A. Ostlie
- *The Physical Universe: An Introduction to Astronomy* by Frank Shu

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# 1. Essential Astronomy

## 1.1 Motivation

Observation is the first step in the scientific process. The more deeply and accurately we observe the nature, the more clues it unravels before us. For instance the observation of the anomalous rate of precession of the perihelion of Mercury's orbit in 1859 became one of the first tests to validate General Relativity as it was not explained by Newton's theory of gravitation. But it works in both ways like earlier it was thought that the beta decay violated law of conservation of energy, but Pauli resolved the issue by suggesting the existence of particles called neutrinos which would have nearly zero rest mass. This was later experimentally validated, and the existence of neutrinos was confirmed. Accurate measurement of parallax distances (first done in 1838 by Friedrich Bessel of star system 61 Cygnet) to nearby stars gave a serious dent geocentric for once and all. In fact the main driver of advancements in astrophysics are ultra-precise telescopes like Hubble and Gaia and one of the most beloved radio telescope (Arecibo Observatory in Peru) which was recently permanently damaged. But we still continue to look beyond the horizons with the new generation of telescopes like the James Webb telescope and HDST.



Figure 1.1: Scientific Process

## 1.2 Objective

But to understand these developments better and appreciate the ingenuity of the people behind them we must get familiar with some basic tools and concepts which are quiet frequently used in astrophysics. So let's start with the coordinate systems: We will discuss basically three commonly encountered coordinate systems: Some basic terminologies to grasp before :

**Equinox:** There are basically two equinoxes Vernal Equinox(March 21) and Autumnal equinox(September 23).They are the period of time when the sun crosses the celestial equator.The day and night are equal in length and both hemispheres of earth receive same energy from sun.

**Elliptic:** It is defined as the plane in which the earth orbits around the sun. Celestial Equator: It is the projection of the equator of earth on the celestial sphere.

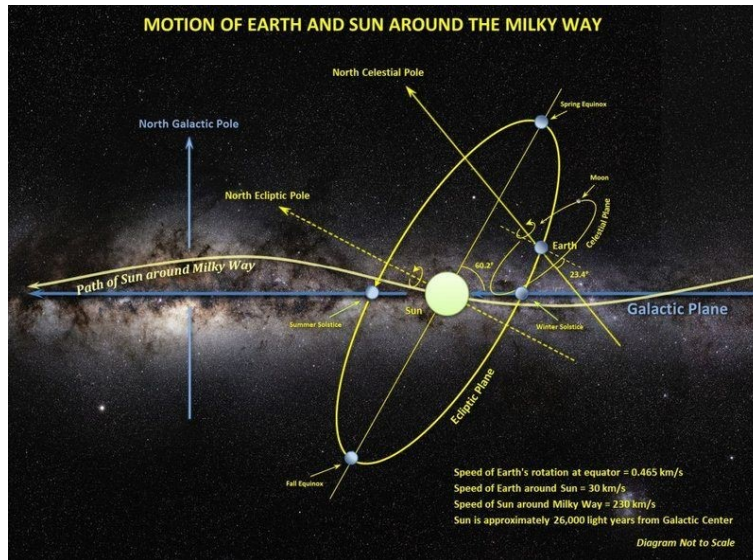


Figure 1.2: A Big picture of motion of Earth through the Universe

## 1.3 Coordinate System

### 1.3.1 Azimuthal System:

It's a relatively simple system but the coordinates of the celestial objects are dependent on our position on earth. The altitude is measured from the apparent horizon of the observer and the azimuth is measured from the local north as shown in the figure

### 1.3.2 Rad-Dec System:

It's a much better system though not as intuitive as Azimuthal system but the coordinate of objects in sky are independent of our position on earth.(Though it is not true on larger time scales due to the effects of precession).In this the reference points are taken from the intersection of celestial equator and ecliptic (i.e the position of sun on vernal equinox)

**Trivia:**The so called north star isn't exactly at the the north pole it is a little of .There are many more stars which are nearer to the north pole than it but none of them are as bright as the north star.Even then the position of the north star is changing continuously due to the effects of precession.



Figure 1.3: Azimuthal Coordinate System

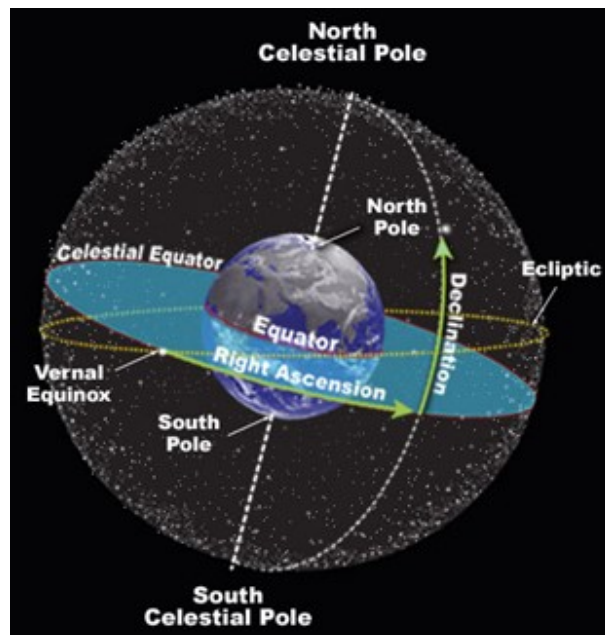


Figure 1.4: Equatorial Coordinate System



### 1.3.3 Galactic Coordinate System:

The galactic coordinate system is a celestial coordinate system in spherical coordinates, with the Sun as its center, the primary direction aligned with the approximate center of the Milky Way Galaxy, and the fundamental plane parallel to an approximation of the galactic plane but offset to its north. It uses the right-handed convention, meaning that coordinates are positive toward the north and toward the east in the fundamental plane.

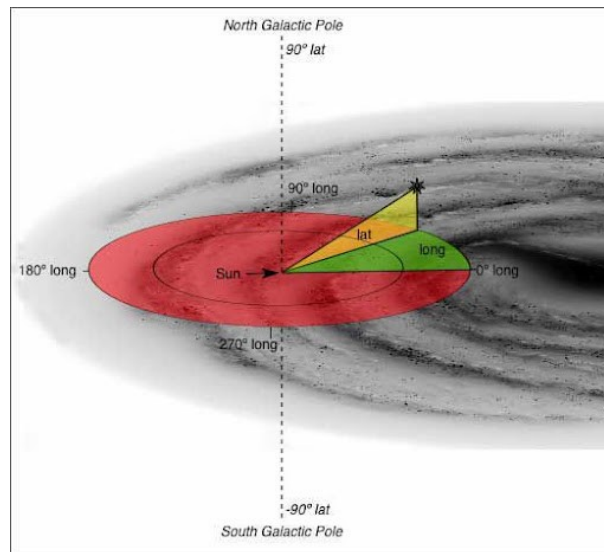


Figure 1.5: Galactic Coordinate System

## 1.4 Some Interesting Phenomena and Tidbits

### 1.4.1 Earth's Axial Precession:

It's a curious phenomenon and due to this even the axis of rotation of earth is not stationary so the so called north star (even now it is not exactly at north pole) will drift away. It takes approximately 26000 years for earth to complete one cycle of precession. So after 13000 years summers in the northern hemisphere will occur in December and winter in June. The cycle of seasons would be reversed! The Greek astronomer Hipparchus was the first to recognize the effects of the precession. The reason for precession is attributed to the deviation of the shape of the earth from a perfect sphere. Since earth is sort of like an oblate spheroid bulging at the equator, the gravitational tidal forces of the Moon and Sun apply torque at the equator, attempting to pull the equatorial bulge into the plane of the elliptic instead causing it to precess. Even planets like Jupiter play a role in this. Due to axial precession of the earth the coordinates of celestial objects change in earth's frame over time so astronomers take this into consideration and apply the necessary corrections.

### 1.4.2 Apsidal Precession:

There is also one other called apsidal precession or the perihelion precession. It is basically the deviation of a planet's trajectory from the ideal ellipse in a flower-petal-like shape. It is due to the gravitational influence of other planets and bodies in the solar system. It cannot be completed

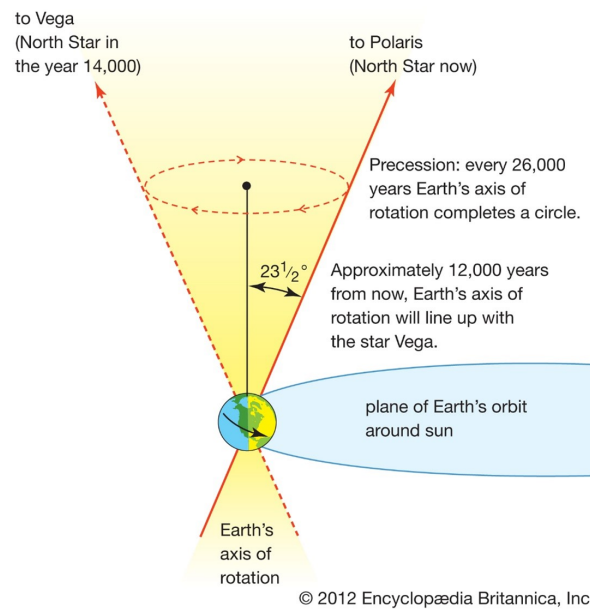


Figure 1.6: Axial Precession

explained with the Newtonian mechanics, general relativity must be invoked to explain it accurately as we discussed above in the case of mercury.

For gaseous planets like Jupiter even tidal perturbations play a significant role.

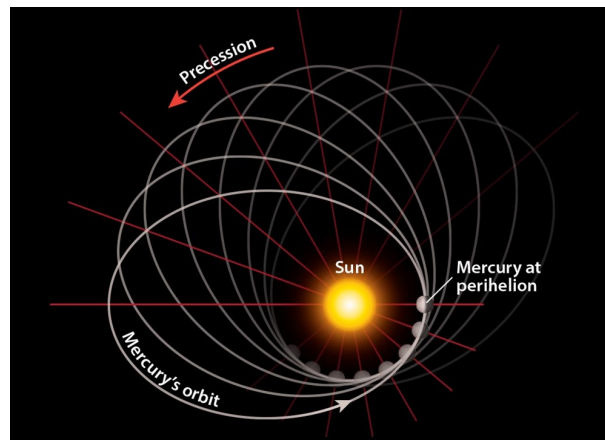


Figure 1.7: Apsidal precession

### 1.4.3 Retrograde Motion:

Retrograde motion is the apparent motion of a planet in a direction opposite to that of other bodies within its system, as observed from a particular vantage point. It is observed only for inner planets. So the astronomical objects near earth orbiting sun exhibit this motion which appears strange at the first site. It appears strange at first site but can be easily explained with the calculation of apparent position considering different angular velocities and distances of the heavenly bodies.

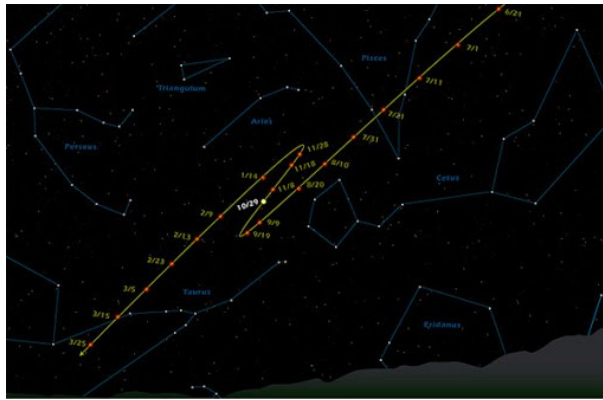


Figure 1.8: Retrograde Motion of Mars

#### 1.4.4 Measurement of Time

Currently we all are using Gregorian calendar (an improvement over Julian calendar taking in account the much more precise period of revolution of earth around sun). Usually events astronomers are interested in require a starting 'zero' time. This time is called the JD 0.0, JD standing for Julian Date. For measuring time as accurately as possible various methods are used like Heliocentric Julian Date and Terrestrial Time.

#### 1.5 Parallax

The **trigonometric parallax** is a method of measuring distances which is particularly useful when the distance to be measured is rather long. It works by measuring the angular position of the object in question from two observation points which are separated by a known distance. Simple trigonometry then tells the distance to the object.

The true scale of the Solar system was first revealed when the distance to Venus was calculated using this method in 1761.

Even the nearest stars are so far away that to get an angle that is measurable by our instruments, locating the two observation points at a distance of Earth's diameter is not enough. We can get a greater baseline distance of the diameter of Earth's orbit by making our observations six months apart. As shown in the figure, a measurement of the parallax angle  $p$  allows us to calculate the distance  $d$  to the star. Since the angle  $p$  is very small, we can approximate  $\tan p$  as  $p$  and hence

$$d = \frac{1}{\tan p} AU \approx \frac{1}{p} AU.$$

Here  $p$  is measured in radians. If we convert  $p$  to *arcseconds* using  $1 \text{ radian} = 206,265''$ , then we get

$$d \approx \frac{206,265}{p''} AU.$$

Defining a new unit of distance, the **parsec** (for parallax-second), as  $1 \text{ pc} = 2.06264806 \times 10^5 \text{ AU} = 3.0856776 \times 10^{16} \text{ m}$  leads to

$$d = \frac{1}{p''} \text{ pc}.$$

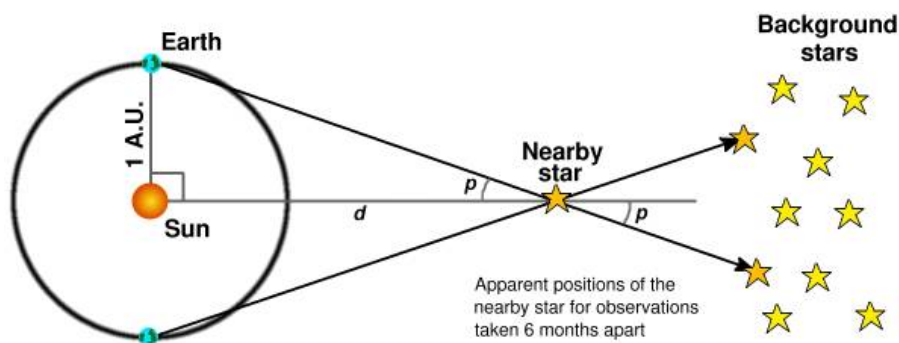


Figure 1.9: Parallax Method

Another unit of distance is the **light-year** which is the distance travelled by light in one Julian year.  $1 \text{ ly} = 9.460730472 \times 10^{15} \text{ m}$ .

Even the nearest star to the Sun, Proxima Centauri, has a parallax angle of only  $0.77''$  and is hence located approximately  $1.3 \text{ pc}$  away from the Sun. Due to such low values of parallax angles of objects in the Universe, their measurement was not possible until the development of better equipment. From 1989 to 1993, the European Space Agency's Hipparcos Space Astrometry Mission was able to measure parallax angles with high accuracies for over 118,000 stars. There was also a lower precision Tycho experiment aboard the spacecraft which was able to measure parallax angles for of more than 1 million stars. However, the distances of stars which this mission was able to catalog is still quite small compared to the  $8 \text{ kpc}$  distance to the centre of our galaxy.

The *Gaia* mission was launched by ESA in 2013 which was able to measure parallax angles with an unprecedented precision. These and upcoming projects will help us in increasing our understanding of the 3D structure of our galaxy.

## 1.6 The Magnitude Scale

### 1.6.1 Apparent Magnitude

The Greek astronomer Hipparchus invented a numerical scale to describe the brightness of each star as seen by us. The brightest stars were assigned **apparent magnitude**  $m = 1$  while the dimmest stars were assigned  $m = 6$ .

Since Hipparchus this scale has been refined on the basis of a theory that human eye recognized a change in brightness when the two brightness in question had a constant ratio in between them. This ratio was obtained based on the observation that a difference of 5 apparent magnitudes corresponded to a factor of 100 in brightness, hence a difference of 1 magnitude corresponds to a factor of  $100^{1/5} \approx 2.512$  in brightness which is the constant ratio. This means that as the magnitude drops by one, the object in question appears 2.512 times more brighter than the other object. Very faint differences in magnitude can now be detected thanks to sensitive detectors. The original scale proposed by Hipparchus has now been extended in both directions from the brightest object in the sky Sun ( $m = -26.83$ ) to approximately  $m = 30$  for the faintest objects detectable. The total range of 57 magnitudes corresponds to nearly 23 orders of difference in brightness of the two extremes.

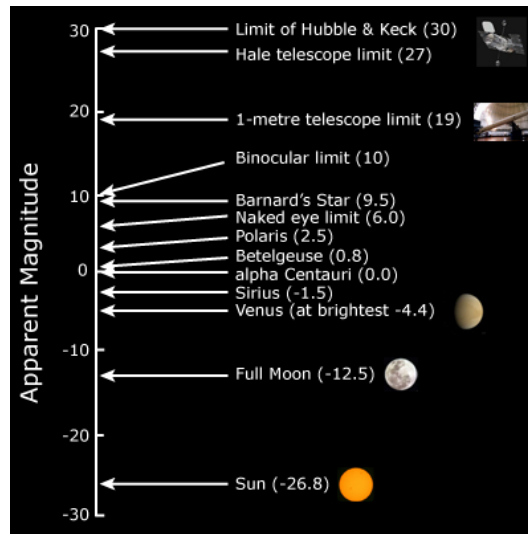


Figure 1.10: Scale of Magnitudes

### 1.6.2 Flux, Luminosity, and the Inverse Square Law

Till now, we were talking about the brightness as perceived by us. The actual brightness of a star is measured in terms of **radiant flux**  $F$  received from it. The radiant flux is the number of joules of starlight energy received per second per unit area. It obviously depends on intrinsically how brightly the star burns (its **luminosity**) but it also depends on the distance of the star from the observer as a star further away would seem less bright.

If we have a star of luminosity  $L$  and we take a spherical shell of radius  $r$  around it then assuming no energy is lost from the star to the shell, the radiant flux  $F$  at a distance  $r$  is given by

$$F = \frac{L}{4\pi r^2}.$$

The luminosity being an intrinsic property makes the radiant flux have an inverse square dependence with the distance from the star. This is the **inverse square** law for light.

### 1.6.3 Absolute magnitude

Earlier we assigned apparent magnitudes to stars but that depends on the distance of the observer as we saw. To set a standard, we define something called the absolute magnitude which is defined as the apparent magnitude a star would have *if* it were located at a distance of 10 pc. Using the fact that a difference of 5 magnitudes between the apparent magnitudes corresponds to a 100 times increase in brightness lets us specify the flux ratio as

$$\frac{F_1}{F_2} = 100^{(m_1 - m_2)/5}.$$

Alternatively, taking logarithms on both sides, we can write

$$m_1 - m_2 = -2.5 \log_{10} \left( \frac{F_1}{F_2} \right).$$

### 1.6.4 Distance Modulus

Using the previously obtained equations and the connection between apparent and absolute magnitudes of a star, we can write,

$$100^{(m-M)/5} = \frac{F_{10}}{F} = \left( \frac{d}{10pc} \right)^2$$

where  $m$  is the apparent magnitude,  $M$  is the absolute magnitude,  $F_{10}$  is the flux that would be received had the star been 10 pc away and  $d$  is the distance of the star. Solving for  $d$  gives

$$d = 10^{(m-M+5)/5}.$$

Since the quantity  $m - M$  decides the star's distance, it is called the star's **distance modulus** and can be given by

$$m - M = 5 \log_{10}(d) - 5.$$

These equations relate the intrinsic properties of a star like luminosity and absolute magnitudes to measurable quantities like radiant flux and apparent magnitudes. Even though the normal way of doing things would be to measure the measurable quantities and then figure out intrinsic properties using the formulas but for certain special kind of stars known as *pulsating variable stars* (these swell and shrink hence changing their brightness and spectrum), it is possible to figure out intrinsic properties without knowing the measurable quantities and hence the distance to these stars can be calculated easily.

## 1.7 The Color Index

The apparent and absolute magnitudes talked about earlier were over all wavelengths of the spectrum and are known as **bolometric magnitudes** (denoted by  $m_{bol}$  and  $M_{bol}$ ). In reality, detectors are only able to measure the radiant flux over a certain range of wavelengths.

### 1.7.1 UVB Wavelength Filters

In the standard UVB system, the star's apparent magnitude is measured through three filters, namely :

- $U$  for the *ultraviolet* magnitude is measured through a filter centered at 65 nm with an effective bandwidth of 68 nm.
- $B$  for the *blue* magnitude is measured through a filter centered at 440 nm with an effective bandwidth of 98 nm.
- $V$  for the *visual* magnitude is measured through a filter centered at 550 nm with an effective bandwidth of 89 nm.

We know that a star's absolute color magnitudes may be determined if its distance  $d$  is known. A star's  $U - B$  color index is defined as the difference in its ultraviolet and blue magnitudes. Similarly, a star's  $B - V$  color index is defined as the difference between its blue and visual magnitudes.

$$U - B = M_U - M_B,$$

and,

$$B - V = M_B - M_V.$$

As mentioned before, more brightness implies lesser magnitude. Hence a star with a smaller  $B - V$  color index is bluer than a star with a larger value of  $B - V$  color index.

The difference between a star's bolometric magnitude and its visual magnitude is its **bolometric correction**  $BC$ :

$$BC = m_{bol} - V = M_{bol} - M_V.$$

For example, Sirius, the brightest appearing star in the sky, with apparent magnitudes  $U = -1.47$ ,  $B = -1.43$  and  $V = -1.44$ , has  $U - B$  color index = -0.04 and  $B - V$  color index = 0.01. As can be seen from the apparent magnitudes, since  $U$  has the least value, Sirius is brightest in the ultraviolet range which is expected for a star with effective temperature of  $T_e = 9970K$ . The bolometric correction for Sirius is -0.09, so its apparent bolometric magnitude is  $m_{bol} = V + BC = -1.53$ . Using the equation  $m_1 - m_2 = -2.5 \log_{10} \left( \frac{F_1}{F_2} \right)$ , we can directly calculate the color magnitudes by knowing the radiant flux as a function of wavelength and the *sensitivity function*  $S(\lambda)$  which is used to describe the fraction of the star's flux that is detected at wavelength  $\lambda$  and hence depends on factors like reflectivity of the telescope, bandwidth of the filters and response of the photometer.

For example, a star's ultraviolet magnitude  $U$  can be given by

$$U = -2.5 \log_{10} \left( \int_0^{\infty} F_{\lambda} S_U d\lambda \right) + C_U,$$

where  $C_U$  is a constant. Similarly, there are expressions for other wavelength magnitudes. The constants in these expressions are chosen so that the star Vega ( $\alpha$  Lyrae) has a magnitude of zero for each filter.

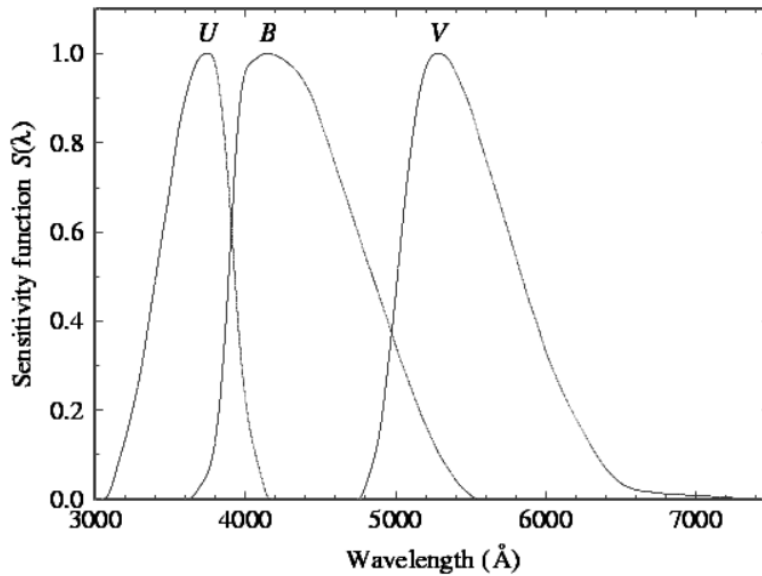


Figure 1.11: Sensitivity functions for U, B and V filters

For a perfect bolometer, capable of detecting 100 percent of light arriving from the star, we set  $S(\lambda) = 1$ , and hence for the bolometric magnitude we have the expression,

$$m_{bol} = -2.5 \log_{10} \left( \int_0^{\infty} F_{\lambda} d\lambda \right) + C_{bol}.$$

$C_{bol}$  was chosen such that the bolometric correction of nearly all stars be negative. From the individual values of  $U, B$  and  $V$ , the color indices are immediately seen to be

$$U - B = -2.5 \log_{10} \left( \frac{\int_0^\infty F_\lambda S_U d\lambda}{\int_0^\infty F_\lambda S_B d\lambda} \right) + C_U - C_B.$$

A similar relation holds for  $B - V$ . Hence, although the apparent magnitudes depend on the star's radius and the distance of the star, the color indices do not since these dependences cancel in the ratio inside the logarithm.

### 1.7.2 The Color Color diagram

The color color diagram is a graph showing the relation between  $U - B$  and  $B - V$  color indices for main-sequence stars. Had the stars been true blackbodies this graph would have been a straight line. However, the stars aren't true blackbodies causing the graph to look as it does. As is shown, very hot stars tend to behave more closely as perfect blackbodies than other stars.

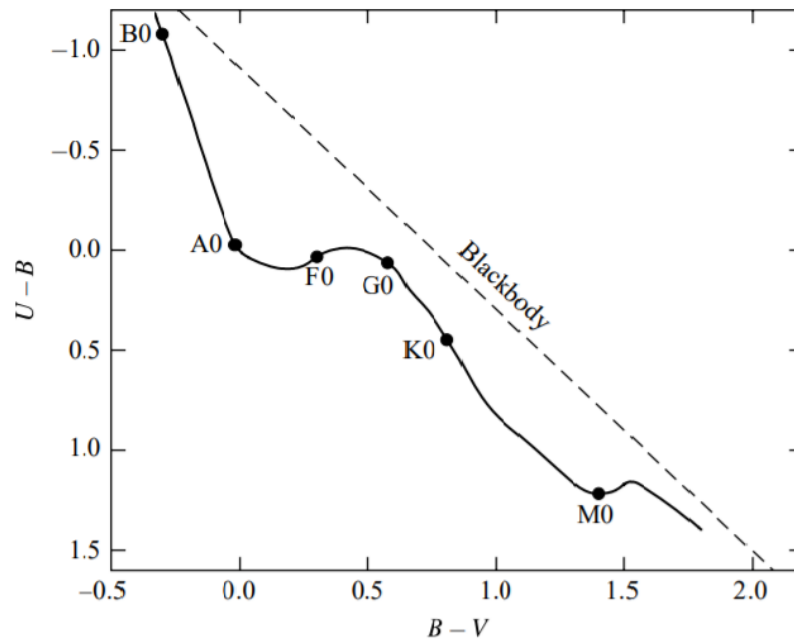


Figure 1.12: Color color diagram for main sequence stars





## 2. Stellar Spectra and Celestial Mechanics

### 2.1 The Formation of Spectral Lines

In 1817, Joseph Fraunhofer had discovered that different stars have different spectra. With the improvement in instruments, increasingly subtle distinctions became possible.

#### The Spectral Types of Stars

A spectral taxonomy was formed at Harvard by Edward C. Pickering and his assistant Williamina P. Fleming in the 1890s, which labeled spectra with capital letters according to the strength of their hydrogen absorption lines, starting with the letter A for the broadest lines. Antonia Maury, Pickering's other assistant, was studying widths of spectral lines. She developed a different classification scheme equivalent to placing Pickering's and Fleming's B class before the A stars. Then, in 1901, Annie Jump Cannon rearranged the sequence of spectra by putting O and B before A and adding decimal subdivisions (e.g., A0–A9).

With the following changes, The Harvard classification scheme of “O B A F G K M” became a temperature sequence, going from the hottest blue O stars to the coolest red M stars. An easy way to remember this is by memorizing the phrase “Oh Be A Fine Girl/Guy, Kiss Me.” Stars closer to the beginning of this sequence are called early-type stars, and those to the end are called late-type stars. Between 1911 and 1914, Cannon classified some 200,000 spectra, and the results were collected into Henry Draper Catalogue.

When an electron jumps from a higher to a lower orbital, emission lines are created. The wavelength of the emitted photon depends on the energies of the atomic orbitals involved in these transitions. Electrons occupy different orbitals in different atmospheres, thus creating distinctions in the spectra of stars.

Table shows the characteristics of various spectral types. It also includes spectral types of brown dwarfs. Brown dwarfs are low mass objects with no nuclear reaction possible, so they are not considered stars in the usual sense. These new spectral types are introduced for objects with low temperatures (1300-2500K for L and less than 1300 K for T spectral types), thus extending the famous phrase to: “Oh Be A Fine Girl/Guy, Kiss Me—Less Talk!”

HARVARD SPECTRAL CLASSIFICATION	
SPECTRAL TYPES	CHARACTERISTICS
<b>O</b>	Hottest blue-white . stars with few lines Strong He II absorption (sometimes emission) lines. He(I)absorption lines becoming stronger.
<b>B</b>	Hot blue-white. He I absorption lines strongest at B2. H(I)(Balmer) absorption lines becoming stronger.
<b>A</b>	White Balmer absorption lines strongest at A0, becoming weaker later. Ca(II) absorption lines becoming stronger.
<b>F</b>	Yellow-white. Ca(II) lines continue to strengthen as Balmer lines continue to weaken. Neutral metal absorption lines (Fe(I), Cr (I)) .
<b>G</b>	Yellow Solar-type spectra. Ca(II) lines continue becoming stronger. Fe (I), other neutral metal lines becoming stronger.
<b>K</b>	Cool orange. Ca(II) H and K lines strongest at K0, becoming weaker later. Spectra dominated by metal absorption lines.
<b>M</b>	Cool red. Spectra dominated by molecular absorption bands, especially titanium oxide (TiO) and vanadium oxide (VO). Neutral metal absorption lines remain strong.
<b>L</b>	Very cool, dark red. Stronger in infrared than visible. Strong molecular absorption bands of metal hydrides (CrH, FeH), water (H <sub>2</sub> O), carbon monoxide (CO), and alkali metals (Na, K, Rb, Cs). TiO and VO are weakening
<b>T</b>	Coollest Infrared. Strong methane (CH <sub>4</sub> ) bands but weakening CO bands.

Figure 2.1: Harvard Spectral Classification

Figures 2.2 and 2.3 show some sample photographic spectra for several spectral types. You will note that hydrogen lines increase in width from O9 to A0, then decrease from A0 through F5, and nearly disappear by K. Helium lines are visible in the early-type stars but begin to vanish in cooler stars.



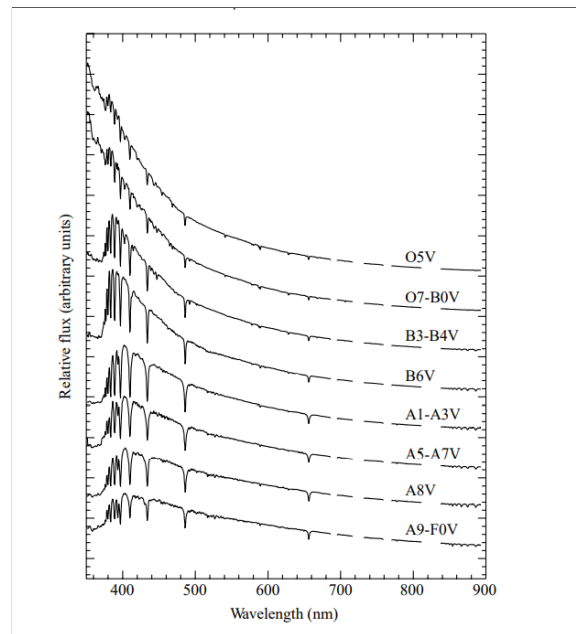


Figure 2.4: Digitized spectra of main sequence classes O5–F0 displayed in terms of relative flux as a function of wavelength. Modern spectra obtained by digital detectors (as opposed to photographic plates) are generally displayed graphically.

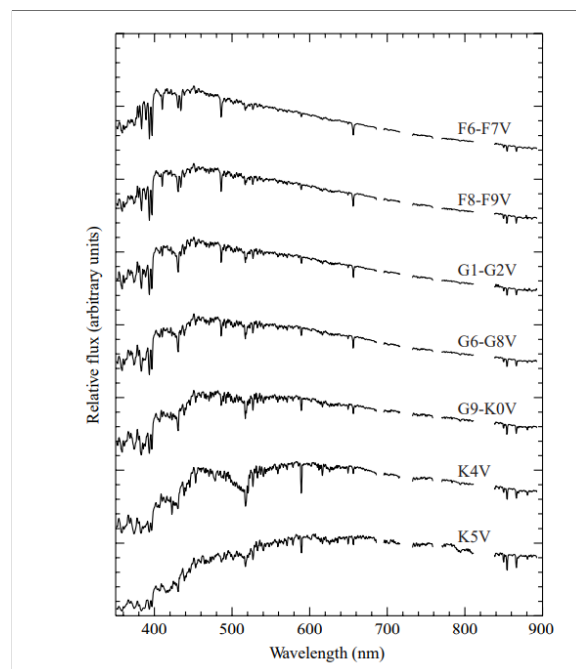


Figure 2.5: Digitized spectra of main sequence classes F6–K5 displayed in terms of relative flux as a function of wavelength.

## 2.2 The Hertzsprung–Russell Diagram

In the 20th century, astronomers came to know about a wide range of stellar luminosities: the total amount of electromagnetic energy emitted per unit of time by a star, galaxy, or astronomical object, and absolute magnitudes. It was known that O stars are hotter and more massive than the M stars, this led to the theory of stellar evolution, which states that each star starts its life as an O star which is massive, hot, and bright blue, but it cools down and become M star as they age off.

If this idea of stellar evolution is correct, there must be a relation between the star's absolute magnitude and spectral type. Hertzsprung discovered that stars of type G had a range of magnitudes, despite having the same spectral classification, and he termed them giant. Russell also independently came to the same conclusion and used the same term. Russell published a diagram, which records a star's observed properties: absolute magnitude and spectral type. In it, more than 200 stars were plotted, most within a band starting from the upper left-hand corner to the lower right-hand corner, i.e., from O to M stars, this band is called the main sequence. The giant stars lie above the lower main sequence and supergiants in the extreme upper right-hand corner. The white dwarf lies below the main sequence.

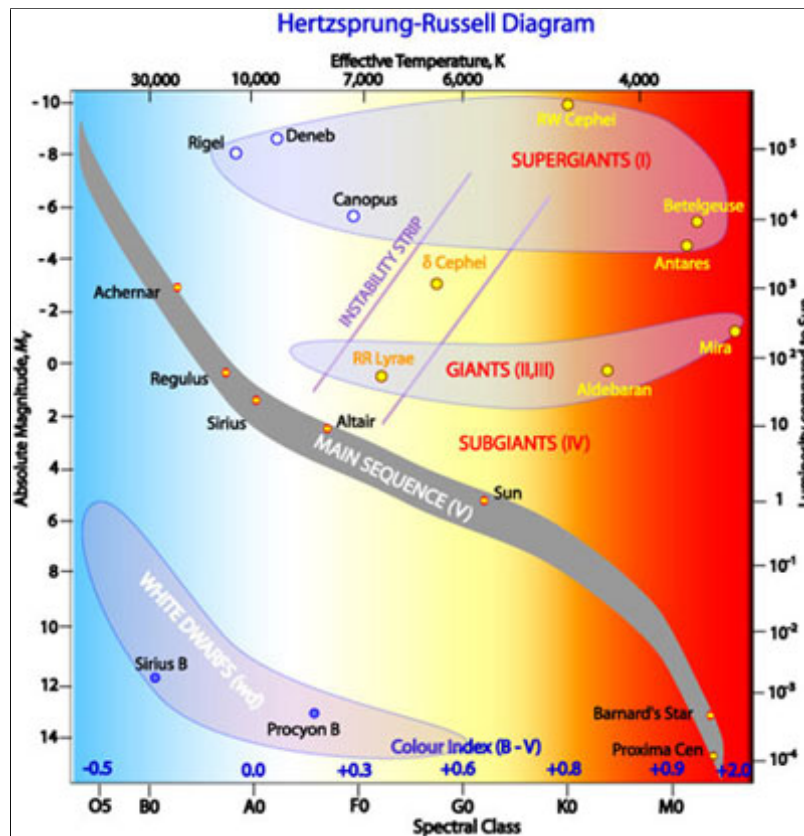


Figure 2.6: An observer's H–R diagram

Figure 2.7 shows another version of the H–R diagram. Here luminosity and effective temperature are plotted for each star instead of absolute magnitude and color index or spectral type. The Sun (G2) is located on the main sequence, as is Vega (A0). You will note that the main sequence is not a line but instead has a finite width.

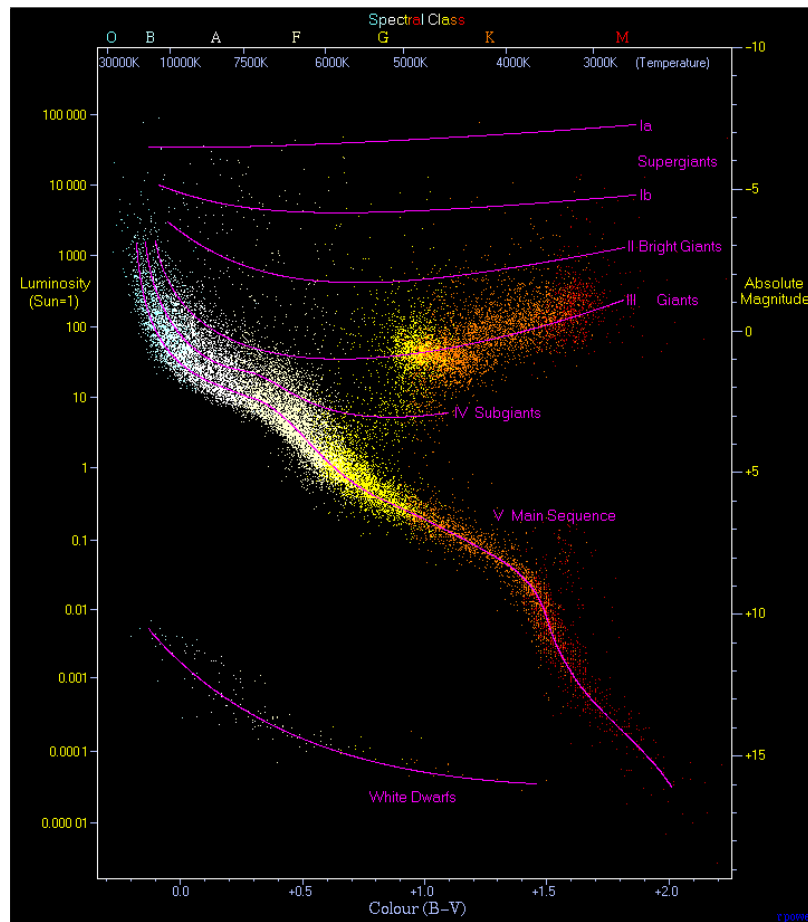


Figure 2.7: The theorist's H–R diagram

We can calculate the radius of the star from its position on the H–R diagram. The size of main-sequence stars ranges from around  $20 R$  to  $0.1 R$  from the extreme upper left end to the lower right end of the main sequence. For giant stars, it is between  $10 R$  and  $100 R$ . Meanwhile, supergiants like Betelgeuse can be 1000 times the sun's radius.

The relation between luminosity and temperature for main sequence stars depends on the star's mass. Most bulky O stars have masses of  $60 M$ , and the lower end of the main sequence having at least  $0.08 M$ . We can calculate the average density of the stars by combining the radii and masses known for main-sequence stars. Main sequence stars have roughly the same density as water. Moving up the main sequence, we observe that massive, early-type stars have a lower average density.

### 2.3 Morgan–Keenan Luminosity Classes

Hertzsprung found a variation showing the difference in the spectra of giant and main-sequence stars of the same spectral type among the spectra of stars cataloged by Antonia Maury. Their work was published in *Atlas of Stellar Spectra*. That consists of 55 prints of spectra that show the effect of temperature and luminosity on stellar spectra. And it includes the criteria for the classification of each spectrum. The MKK Atlas established the two-dimensional M–K (Morgan–Keenan) system of

spectral classification. The two-dimensional M-K classification scheme enables astronomers to locate a star's position on the H-R diagram based entirely on its spectral appearance. Later a luminosity class is added to a star's Harvard spectral type denoted by a Roman numeral. "I" for the supergiant stars, and "V" denotes a main-sequence star.

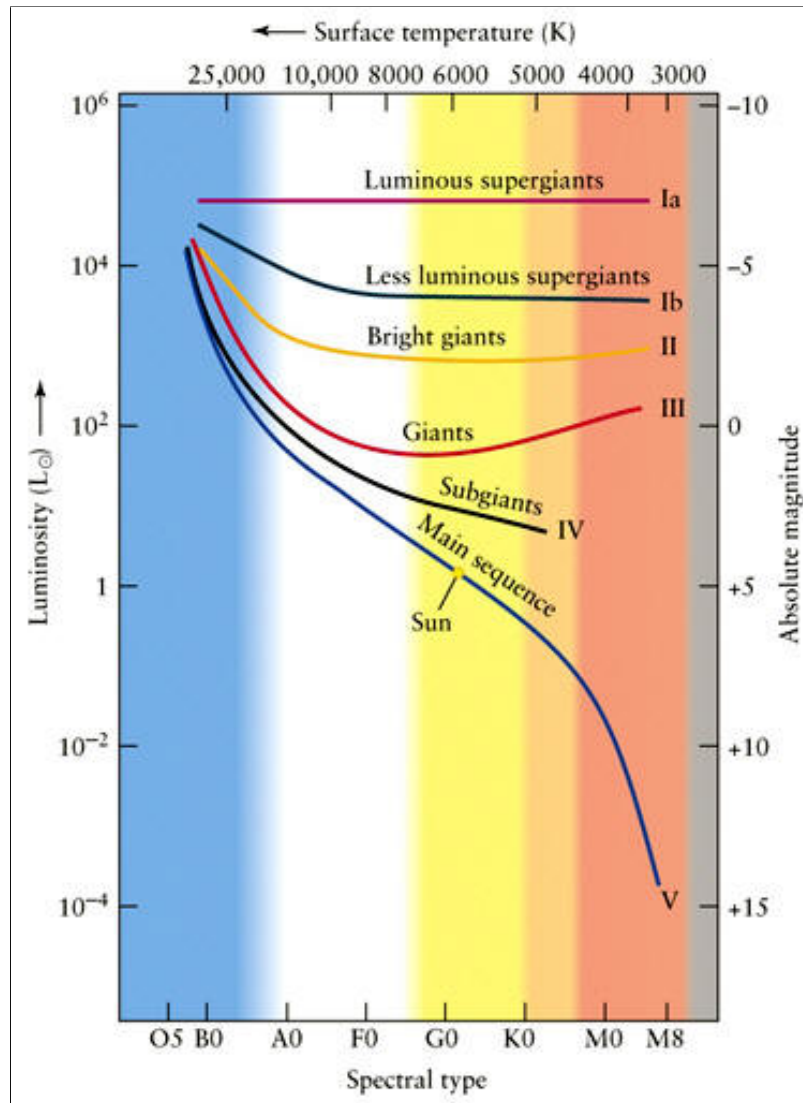


Figure 2.8: Morgan–Keenan Luminosity Classes

## 2.4 Elliptical Orbits

The idea of a heliocentric universe was not immediately accepted, it lacked the support of observations capable of unambiguously demonstrating that a geometric model was wrong. After the death of Copernicus, Tycho Brahe carefully followed the motions of the wandering stars and other celestial objects. He is credited with observing the supernova of 1572, which clearly demonstrated that the heavens were not unchanging as Church doctrine held. Tycho was not able to find any clear

evidence of the motion of Earth through the heavens, therefore he concluded that the Copernicus model must be false.

### Kepler's Laws of Planetary Motion

Johannes Kepler joined Tycho in his invitation, Kepler was a heliocentrist and it was his desire to find a geometric model of the universe that would be consistent with the best observations then available. Kepler's initial idea was that the universe is arranged with five perfect solids, nested to support the six-known naked-eye planets on a crystalline sphere, with the entire system centered on the Sun but this model proved unsuccessful. He attempted to devise an accurate set of circular planetary orbits about the Sun, focusing specifically on Mars. Believing that Tycho wouldn't have made observational errors, Kepler felt forced to dismiss the idea of purely circular motion. Kepler began to consider the possibility that planetary orbits were elliptical in shape rather than circular. Through this relatively minor mathematical change, he was finally able to bring all of Tycho's observations into an agreement with a model for planetary motion. This paradigm shift also allowed Kepler to discover that the orbital speed of a planet is not constant but varies in a precise way depending on its location in its orbit.

**Kepler's First Law-** A planet orbits the Sun in an ellipse, with the Sun at one focus of the ellipse.

**Kepler's Second Law-** A line connecting a planet to the Sun sweeps out equal areas in equal time intervals.

**Kepler's Third Law-** The Harmonic Law:

$$P^2 = a^3$$

,where  $P$  is the orbital period of the planet and  $a$  is the average distance of the planet from the Sun. This law relates the average orbital distance of a planet from the Sun to its sidereal period.

### The Geometry of Elliptical Motion

An ellipse is defined by that set of points that satisfies the equation  $r + r' = 2a$ , where  $a$  is a constant known as semi major axis and  $r$  and  $r'$  represent the distances to the ellipse from the two focal points,  $F$  and  $F'$  respectively.

According to Kepler's first law, a planet orbits the Sun in an ellipse, with the Sun located at one focus of the ellipse, the principal focus,  $F$ , and the other focus is empty. If  $F$  and  $F'$  were located at the same point then  $r = r' = a$ , the equation for a circle. The distance  $b$  is known as the semi major axis. The eccentricity,  $e$ , of an ellipse is defined as the distance of either focal point from the center of the ellipse may be expressed as  $ae$ . The point on the ellipse that is closest to the principal focus is called perihelion, and the point on the opposite end of the major axis and farthest from the principal focus is known as aphelion.

Kepler's second law stated that the orbital speed of a planet depends on its location in that orbit.

## 2.5 Newtonian Mechanics

### The observation of Galileo

When Kepler was developing his three laws of planetary motion, Galileo Galilei was studying the motion of objects on Earth. Galileo is the father of modern observational astronomy. He made several observations in support of the heliocentric model of the universe.



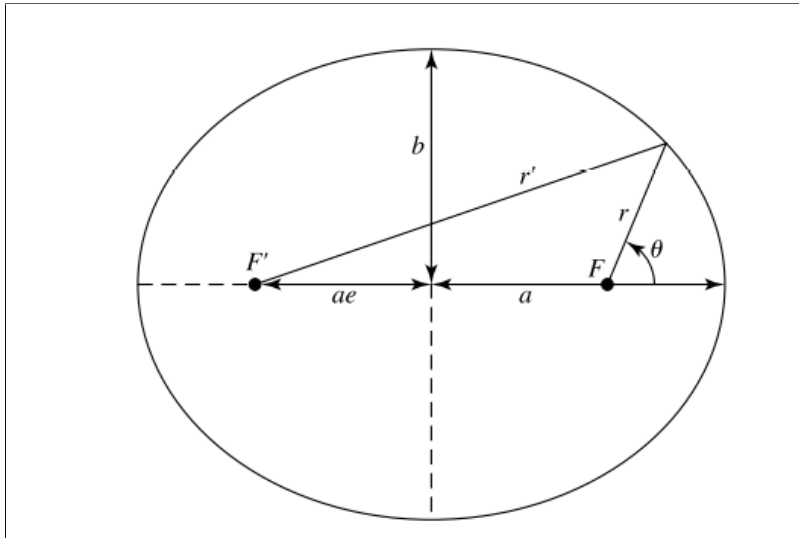


Figure 2.9: The geometry of an elliptical orbit.

### Newton's Three Laws of Motion

Isaac Newton, arguably the greatest of any scientific mind in history, was born on Christmas Day in the year of Galileo's death. After graduation, while living at home in Woolsthorpe away from the immediate dangers of the Plague, during this period he made significant discoveries and theoretical advances in understanding motion, astronomy, optics, and mathematics. Today's classical mechanics is described by Newton's three laws of motion, along with his universal law of gravity.

**Newton's First law of motion** : A body at rest will remain at rest and a body in motion will remain in motion in a straight line at a constant speed unless acted by an external force.

The first law may be stated in terms of the momentum of an object,  $p = mv$ , where  $m$  and  $v$  are mass and velocity respectively.

**Newton's Second law of motion** : The net force acting on an object is proportional to its mass and resultant acceleration.

Assuming that the mass is constant and using the definition  $a = dv/dt$ , second law may also be expressed as  $F_{net} = mdv/dt = d(mv)/dt = dp/dt$ . The net force on an object is equal to the time rate of change of momentum.

**Newton's Third law of motion** : For every action, there is an equal and opposite reaction.

In this law, action and reaction are understood as forces acting on different objects.

## 2.6 Newton's Law of Universal Gravitation

Using his three laws of motion along with Kepler's third law of planetary motion, Newton was able to find an expression describing the force that holds planets in orbits.

The expression of the law of gravitation is:

$$F = GMm/r^2, \quad \text{where } G = 6.67310^{-11} \text{ Nm}^2 \text{ kg}^{-2}$$

(Universal Gravitational Constant) and  $M$  and  $m$  are masses of two bodies and  $r$  is the distance between them.

Newton's law of gravity applies to any two objects having mass. For an extended object, the force exerted by that object on another extended object may be found by integrating over each of their mass distributions.

When an object is dropped near the surface of Earth, it accelerates towards the center of Earth at the rate of  $g = 9.80ms^{-2}$ , the local acceleration of gravity. Using Newton's second law and his law of gravity, the expression for gravity acceleration may be found. The force of gravity on  $m$  due to Earth is given by  $F = GMm/(R + h)^2$  where  $M$  and  $R$  are mass and radius of Earth respectively and  $h$  is the height of an object above Earth's surface.

### Work and Energy

In physics, it is very helpful to have some understanding of the energies of specific physical phenomenon. The amount of energy necessary to raise an object of mass  $m$  a height  $h$  against a gravitational force equals the change in the system's potential energy. Since only relative changes in potential energy are physically meaningful, a reference position where the potential energy is defined as being identically zero may be chosen. The quantity

$$K = mv^2/2$$

is referred to as the kinetic energy of the object.

The total energy of an object i.e. kinetic and potential energy is conserved and this is the law of conservation of energy.



## 3. Binary Systems

### 3.1 Binary Stars and its Classification

The term binary star was coined by Sir William Herschel in 1802 to designate, in his definition, "a real double star - the union of two stars that are formed together in one system by the laws of attraction". Any two closely-spaced stars might appear to be a double star, the most famous case being Mizar and Alcor in the Big Dipper. Herschel, in 1780, measured the separation and orientations of over 700 pairs that appeared to be binary systems, and found that about 50 pairs changed orientation over two decades of observation.

Binary star is a system of two stars in which one star revolves around the other or both revolve around a common center. A true binary is a pair of stars bound together by gravity. At least half of all "stars" in the sky are actually multiple systems, two or more stars in orbit about a common center of mass. Analysis of the orbital parameters of these systems provides vital information about a variety of stellar characteristics, including mass.

#### Optical double

These systems are not actually binaries at all but simply two stars that lie along the same line of sight. These are just chance superpositions of two stars on the sky. They do not lie the same distance away from us. Like the stars which form a constellation, they are not really neighbours. As the stars are not gravitationally bound, and hence the system is not useful in determining stellar masses.

#### Visual binary

A visual binary is a gravitationally bound binary star system that can be resolved into two stars. These stars are estimated, via Kepler's 3rd law, to have periods ranging from a few years to thousands of years. A visual binary consists of two stars, usually of a different brightness. Because of this, the brighter star is called the primary and the fainter one is called the companion. If the primary is too bright, relative to the companion, this can cause a glare making it difficult to resolve the two components. However, it is possible to resolve the system if observations of the brighter star show it to wobble about a centre of mass. In general, a visual binary can be resolved into two stars with a

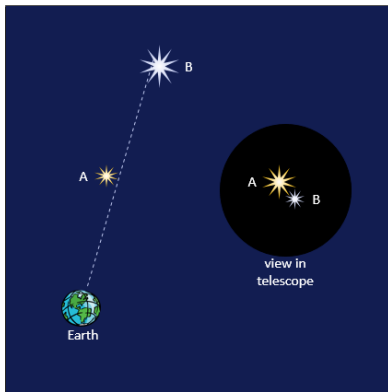


Figure 3.1: Optical Double

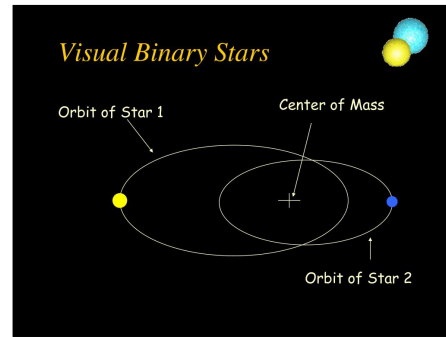


Figure 3.2: Visual Binary

telescope if their centres are separated by a value greater than or equal to one arcsecond, but with modern professional telescopes, interferometry, or space-based equipment, stars can be resolved at closer distances.

### Astrometric binary

Astronomers have discovered some stars that seemingly orbit around an empty space. Astrometric binaries are relatively nearby stars which can be seen to wobble around a point in space, with no visible companion. The companion could be very dim, so that it is currently undetectable or masked by the glare of its primary, or it could be an object that emits little or no electromagnetic radiation, for example a neutron star. The visible star's position is carefully measured and detected to vary, due to the gravitational influence from its counterpart. The position of the star is repeatedly measured relative to more distant stars, and then checked for periodic shifts in position. Typically this type of measurement can only be performed on nearby stars, such as those within 10 parsecs. Nearby stars often have a relatively high proper motion, so astrometric binaries will appear to follow a wobbly path across the sky.

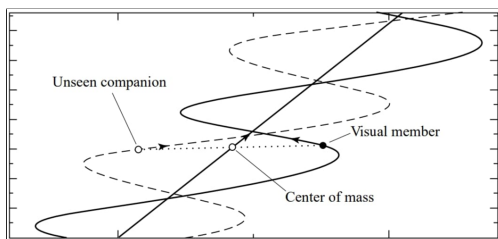


Figure 3.3: Astrometric Binary

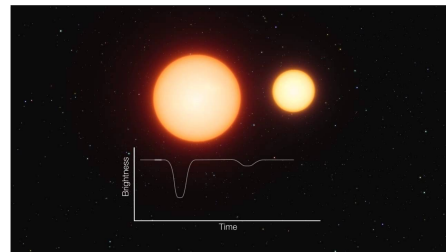


Figure 3.4: Eclipsing Binary

### Eclipsing binary

An eclipsing binary star is a binary star system in which the orbit plane of the two stars lies so nearly in the line of sight of the observer that the components undergo mutual eclipses. Algol, a triple star system in the constellation Perseus, contains the best-known example of an eclipsing binary. Eclipsing binaries are variable stars, not because the light of the individual components

vary but because of the eclipses. The light curve of an eclipsing binary is characterized by periods of practically constant light, with periodic drops in intensity when one star passes in front of the other. An eclipsing binary's period of orbit may be determined from a study of its light curve, and the relative sizes of the individual stars can be determined in terms of the radius of the orbit, by observing how quickly the brightness changes as the disc of the nearest star slides over the disc of the other star.

### Spectrum binary

A spectrum binary is a system with two superimposed, independent, discernible spectra. The Doppler effect causes the spectral lines of a star to be shifted from their rest frame wavelengths if that star has a nonzero radial velocity. Since the stars in a binary system are constantly in motion about their mutual center of mass, there must necessarily be periodic shifts in the wavelength of every spectral line of each star (unless the orbital plane is exactly perpendicular to the line of sight, of course). It is also apparent that when the lines of one star are blueshifted, the lines of the other must be redshifted relative to the wavelengths that would be produced if the stars were moving with the constant velocity of the center of mass. However, it may be that the orbital period is so long that the time dependence of the spectral wavelengths is not readily apparent. In any case, if one star is not overwhelmingly more luminous than its companion and if it is not possible to resolve each star separately, it may still be possible to recognize the object as a binary system by observing the superimposed and oppositely Doppler-shifted spectra.

### Spectroscopic binary

In these systems, the separation between the stars is usually very small, and the orbital velocity very high. Unless the plane of the orbit happens to be perpendicular to the line of sight, the orbital velocities will have components in the line of sight and the observed radial velocity of the system will vary periodically. Since radial velocity can be measured with a spectrometer by observing the Doppler shift of the stars' spectral lines, the binaries detected in this manner are known as spectroscopic binaries. Most of these cannot be resolved as a visual binary, even with telescopes of the highest existing resolving power.

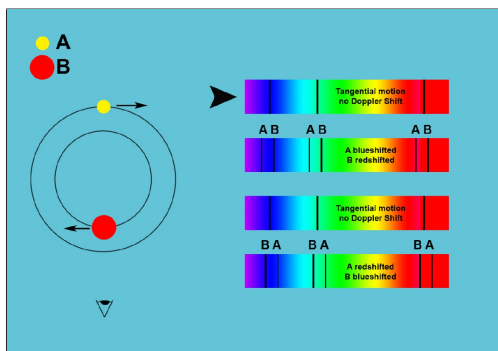


Figure 3.5: Spectrum Binary



Figure 3.6: Spectroscopic Binary(Mizar A)

### 3.2 Mass determination using Visual Binaries

Binary systems are particularly important here because they are orbiting each other, their gravitational interaction can be studied by observing parameters of their orbit around each other and the centre of mass. Before applying Kepler's 3rd Law, the inclination of the orbit of the visual binary must be taken into account. Relative to an observer on Earth, the orbital plane will usually be tilted. If it is at  $0^\circ$  the planes will be seen to coincide and if at  $90^\circ$  they will be seen edge on. Due to this inclination, the elliptical true orbit will project an elliptical apparent orbit onto the plane of the sky. Kepler's 3rd law still holds but with a constant of proportionality that changes with respect to the elliptical apparent orbit. The inclination of the orbit can be determined by measuring the separation between the primary star and the apparent focus. Once this information is known the true eccentricity and the true semi-major axis can be calculated since the apparent orbit will be shorter than the true orbit, assuming an inclination greater than  $0^\circ$ , and this effect can be corrected for using simple geometry.

$$a = \frac{a''}{p''}$$

Where  $a''$  is the true semi-major axis and  $p''$  is the parallax.

Once the true orbit is known, Kepler's 3rd law can be applied. We re-write it in terms of the observable quantities such that

$$(m_1 + m_2)T^2 = \frac{4\pi^2(a''/p'')^3}{G}$$

From this equation we obtain the sum of the masses involved in the binary system. Remembering a previous equation we derived,

$$r_1 m_1 = r_2 m_2$$

we can solve the ratio of the semi-major axis and therefore a ratio for the two masses since

$$\frac{a_1''}{a_2''} = \frac{a_1}{a_2} \text{ and } \frac{a_1}{a_2} = \frac{m_2}{m_1}$$

The individual masses of the stars follow from these ratios and knowing the separation between each star and the centre of mass of the system

### 3.3 Eclipsing, Spectroscopic Binaries

The Effect of Eccentricity on Radial Velocity Measurements The radial velocity method allow us to measure the eccentricity of the orbit, because of variations in orbital velocity around the elliptical orbit (Kepler's laws). Depending on eccentricity of the orbit and viewing angle, can get different

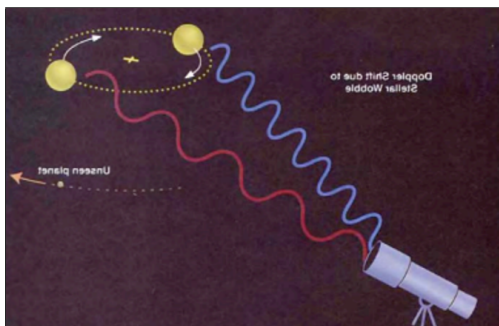


Figure 3.7: Periodic Doppler effect due to orbital motion

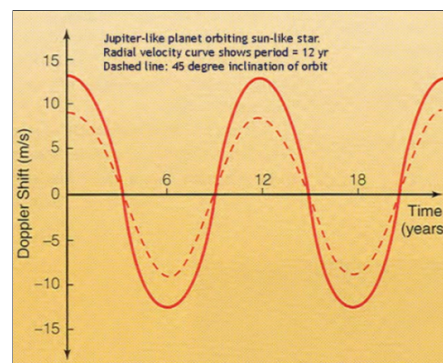
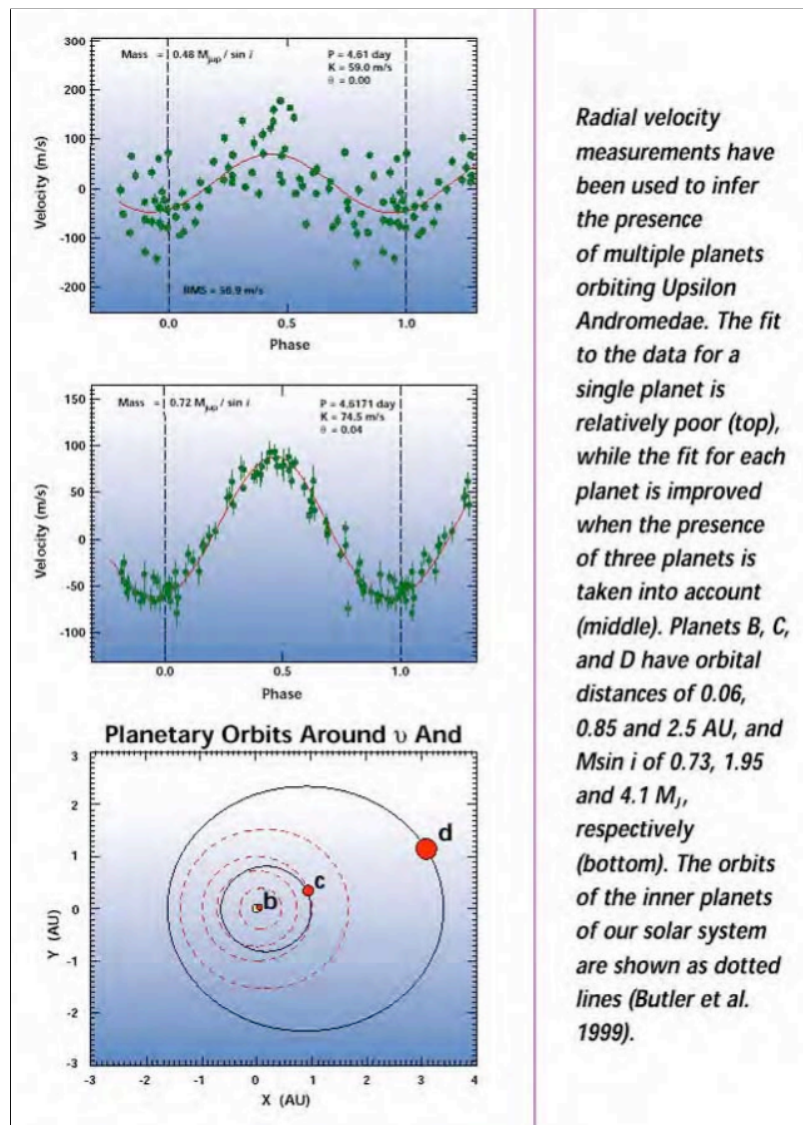


Figure 3.8: Resulting radial velocity curve

forms of the radial velocity curve. Radial velocity method: Search for periodic radial velocity variation in parent star. Depending on eccentricity of the orbit and viewing angle, can get different forms of the radial velocity curve. The surprising thing is that there are any giant planets with such eccentric orbits. Gravitational forces should “circularize” orbits over time. This could be bad news for the survival of Earth-like planets.

The radial velocity method allow us to measure the eccentricity of the orbit, because of variations in orbital velocity around the elliptical orbit (Kepler’s laws).



### 3.3.1 The Mass Function and the Mass–Luminosity Relation

The study of binary stars provides the key piece of information to understanding why main sequence stars have a range of properties from high luminosity to low luminosity. Orbital periods and orbital radii via Kepler’s Third Law yields the mass of stars. When the luminosity of main sequence stars is plotted against their masses, we observe a mass-luminosity relationship, approximately of the

form  $L \propto M^{3.5}$ . In other words, doubling the mass of a main sequence star produces an increase in luminosity by a factor  $2^{3.5} = 11$  times. The Main Sequence is therefore a mass sequence, with low mass stars forming an equilibrium with a cool surface and a low luminosity (low energy generation rate), and high mass stars having hot surfaces and high luminosity (larger energy generation rate). The mass-luminosity relation holds only for main sequence stars. Two giant or supergiant stars with the same luminosities and surface temperatures may have dramatically different masses. The fact that luminosity is not directly proportional to mass produces a major problem for observing and interpreting the universe. This problem can be seen by considering the masses, luminosities, and mass-luminosity ratios  $\frac{M}{L}$  for different types of stars.

### 3.3.2 Using Eclipses to Determine Radii and Ratios of Temperatures

The ratio of effective temperatures of two stars can be obtained from the light curve of an eclipsing binary. By considering objects as blackbody radiators and comparing amount of light received during an eclipse with the amount received when both members are fully visible.

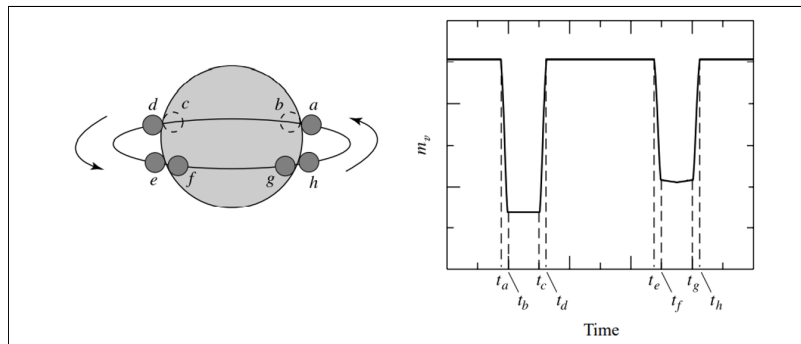
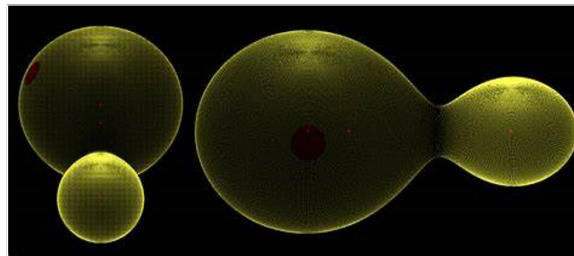


Figure 3.9: The light curve of an eclipsing binary for which  $i = 90^\circ$ . The times indicated on the light curve correspond to the positions of the smaller star relative to its larger companion. It is assumed in this example that the smaller star is hotter than the larger one.

### 3.3.3 A Computer Modelling Approach

It's a modern approach used to analyse the data that comes from binary star systems. The detailed



models involved in this gives us info about a variety of physical parameters including masses, radii, effective temperatures and many more details. Due to gravitational forces, combined with the effects of rotational and orbital motion, the shape of star changes from spherical to a bit elongated.



### 3.4 Search of Extrasolar Planets

During the recent decade, the question of the existence of planets orbiting stars other than our Sun has been answered unequivocally. Extrasolar planets were first discovered in 1992. About 150 extrasolar planets have been detected since 1995, and their properties are the subject of wide interest in the research community. Planet formation and evolution theories are adjusting to the constantly emerging data, and astronomers are seeking new ways to widen the sample and enrich the data about the known planets. More than 4,000 are known, and about 6,000 await further confirmation. In September 2002, ISSI organized a workshop focusing on the physics of “Planetary Systems and Planets in Systems”<sup>1</sup>. The present contribution is an attempt to give a broader overview of the researches in the field of exoplanets and results obtained in the decade after the discovery of the planet 51 Peg b. The existence of planets orbiting other stars was speculated upon even in the

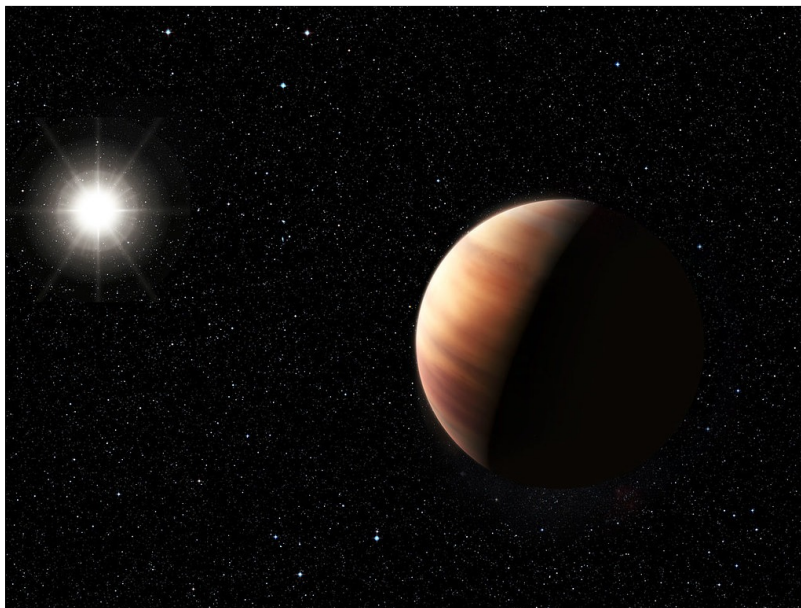


Figure 3.10: 51 Pegasi B

4th century BC, when Epicurus and Aristotle debated it using their early notions about our world. Epicurus claimed that the infinity of the Universe compelled the existence of other worlds. After the Copernican Revolution, Giordano Bruno wrote: “Innumerable suns exist; innumerable earths revolve around these suns in a manner similar to the way the seven planets revolve around our Sun”. Because planets are much fainter than the stars they orbit, extrasolar planets are extremely difficult to

METHOD	RADIAL VELOCITY	TRANSIT	DIRECT IMAGING	GRAVITATIONAL MICROLENSING	ASTROMETRY
WAY	Watching for Wobble	Searching for Shadows	Taking Pictures	Light in a Gravity Lens	Minuscule Movements
PLANETS DISCOVERED	864 planets	3343 planets	53 planets	108 planets	1 planet

Figure 3.11: 5 Ways to Find a Planet

detect directly. By far the most successful technique for finding and studying extrasolar planets has been the radial velocity method, which measures the motion of host stars in response to gravitational tugs by their planets.

Swiss astronomers Michel Mayor and Didier Queloz discovered the first planet using this technique, 51 Pegasi b, in 1995.

The first extrasolar planetary transits that were discovered were those of HD209458 b. Mazeh et al.<sup>41</sup> first discovered the planet in the traditional radial-velocity technique. Soon after the radial-velocity detection, Charbonneau et al.<sup>42</sup> and Henry et al.<sup>43</sup> detected the periodical dimming of the light, with exactly the same period as the radial-velocity variations, of 3.52 days (Fig. 7a). The two teams detected the transits using small and relatively cheap telescopes, which demonstrated that achieving the required photometric precision by ground-based observations was realistic. HD209458 b, being the first transiting extrasolar planet, demonstrates the scientific potential of transit.

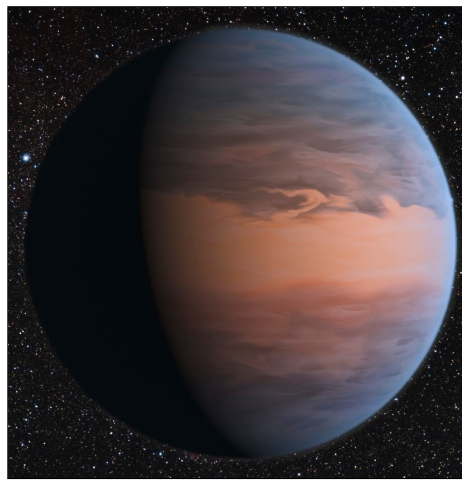


Figure 3.12: HD209458 b

After the first detection of transits, numerous surveys to look for others were initiated by several groups. One such survey is the Optical Gravitational Lensing Experiment (OGLE), a project that monitors dense stellar fields in search of another exotic effect – gravitational lenses<sup>50</sup>. Currently, already six transiting planets are known, four of them from the OGLE project.

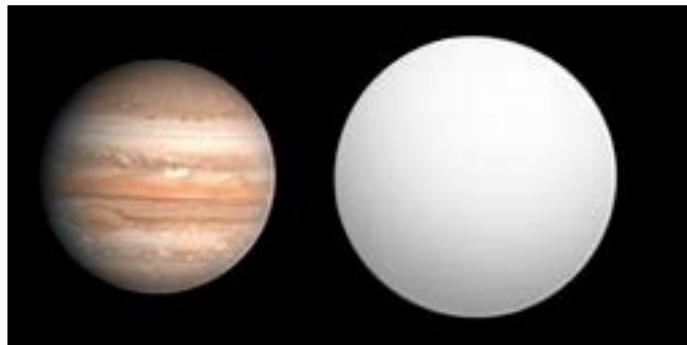


Figure 3.13: Ogle TR 56b

## 4. Galaxies

### 4.1 Introduction

Galaxies are gravitationally bound collection of stars and interstellar matter. These are the building blocks of universe at large scale .Most of the galaxies are organized into groups. We live in [Milky Way](#), a part of Local Group, with [Andromeda](#) as its neighbour. There are many galaxies besides ours, though. There are so many, we can't even count them all yet! The Hubble Space telescope looked at a small patch of space for 12 days and found 10,000 galaxies, of all sizes, shapes, and colors. Some scientists think there could be as many as one hundred billion galaxies in the universe



Figure 4.1: Andromeda Galaxy



Figure 4.2: Galaxy cluster

By studying the physical properties of galaxies we can understand about its evolution and formation and based on that we classify galaxies. Though the traditional classification of galaxies is subjective and based on appearances , not physical properties and Incomplete because it misses the major separation of dwarfs and giants.

### 4.2 Morphological Classification and Galaxy Types

This morphological classification scheme, known as the Hubble sequence, divides galaxies into ellipticals , spirals, and irregulars . The spirals are further subdivided into two parallel sequences, the normal spirals , and the barred spirals . A transitional class of galaxies between ellipticals and spirals,

known as lenticulars, can be either normal or barred . Hubble then arranged his morphological sequence in the form of a tuning-fork diagram Previously galaxies were divided based on their appearances and shape e.g, Hubble Scheme ( [tuning fork diagram](#) Fig3) but modern classification is based on their physical properties and this also help us in understanding origin and proprieties of subsystems like disks,halos etc.

### Hubble's Classification

Hubble observed the shape of galaxies and gave their names accordingly like Elliptical , Spiral, Barred , Lenticular etc. and thought that this shows an evolutionary pattern. Hubble originally thought (incorrectly) that the tuning-fork diagram could be interpreted as an evolutionary sequence for galaxies. As a result, he referred to galaxies toward the left of the diagram as early types and to those toward the right as late types , terminology that is still in widespread use today .Hubble sequence is represented in the form of a tuning fork(Fig3) with elliptical galaxies on the left and barred and unbarred spirals are along the two parallel lines of the fork ; Lenticulars are placed in between spirals and ellipticals .We can further classify elliptical ones based on Ellipticity ( $=1 - \frac{b}{a}$  ;  $a$  and  $b$  : major and minor axes of ellipse), which increases as we go from left to right along tuning fork. A typical elliptical galaxy is mainly composed of stars, hot ionized gas and dark matter whereas A typical spiral or disk galaxy is made up of stars, interstellar gas (both ionized and neutral gas (mainly hydrogen denoted by HI and ionized H gas by HII), interstellar dust and dark matter.

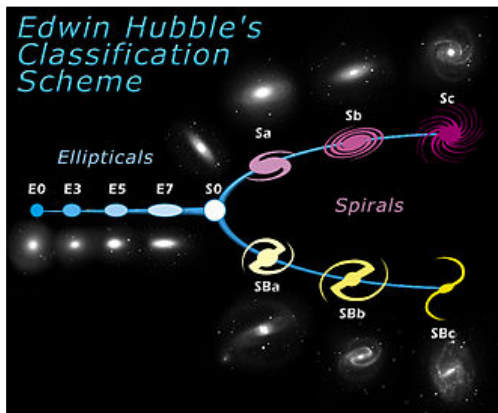


Figure 4.3: Tuning Fork Model

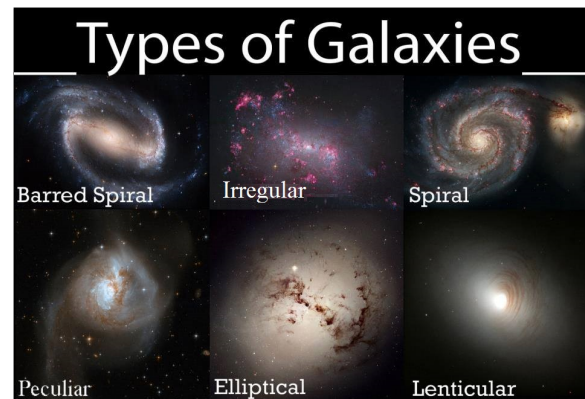


Figure 4.4: Galaxy shapes

### Trends along the Hubble Sequence

Hubble Sequence gives us a trend in star formation histories for e.g, Elliptical galaxies appear uniform because they are older galaxies which have used up their gas and have older stars. Similarly Spiral galaxies are comparatively younger and are still forming stars at a few solar mass per year .

### Spiral Galaxies

These are like disks embedded in halos .The stars in spiral galaxies are in disks and are supported by rotational motion about their galaxy centers. It is composed of a disk of stars and gas that are embedded in a very massive dark matter halo. There maybe a bulge in the center of the disk and an elongated feature called a bar. There are compact old, star clusters called globular clusters in the halo.

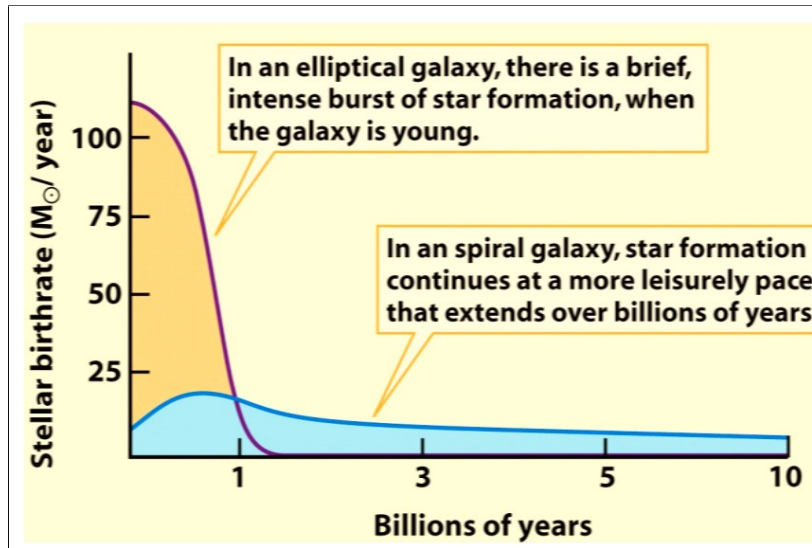


Figure 4.5: Star Formation History in Galaxies

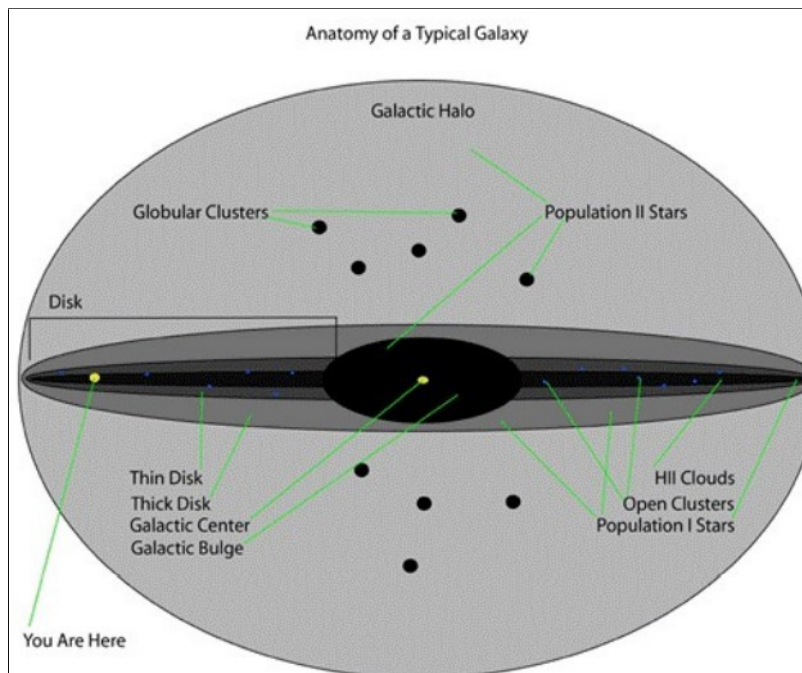


Figure 4.6: Our Galaxy Structure(Image credit: astronomyonline.org)

### Elliptical Galaxies

The stars in these are embedded in a very massive dark matter halo. There may small nuclear disks of dust and gas, possibly due to mergers. They are often surrounded by massive halos of hot gas emitting in X-rays. The gas is a remnant from early star formation. They have the most massive nuclear black holes (10<sup>7</sup> to 10<sup>10</sup> solar mass) in the Universe. A good example is M87, the nearest elliptical galaxy. They show the high nuclear activity due to accretion onto the supermassive black

holes (SMBHs). Quasar host galaxies are ellipticals. They often have radio jets. They show emission in the highest frequencies – gamma rays and X-rays.



Figure 4.7: Centaurus Galaxy (with jets overlaid)(Image credit : apod.nasa.gov)

Ellipticity of these galaxy is not intrinsic but observer dependent. They are actually Triaxial Ellipsoids in 3-D space. It is due to the anisotropic velocity dispersion of stellar motion, which stretch the galaxies in proportion along their 3 principle axes. Thus, elliptical galaxies are not flattened only by rotation. Most of the kinetics energy is in random motions. More massive ellipticals tend to be more anisotropic.

### Barred Galaxies

Half of all disk galaxies- Milky Way included - show a central bar which contain up to 1/3 of the total light. Bars are a form of dynamical instability in differentially rotating stellar disks. Presence of a dark halo stabilizes the disks against the formation, so disks are marginally unstable. Bars are not density wave; they rotate with a pattern speed, and stars in the bar stay in the bar. They can funnel gas to the centre of the galaxy

### Lenticular Galaxies

A Lenticular galaxy (denoted S0) is a type of galaxy intermediate between an elliptical and a spiral galaxy in galaxy morphological classification scheme. It contains a large-scale disc but does not have large-scale spiral arms. Lenticular galaxies are galaxies that have used up or lost most of their interstellar matter and therefore have very little ongoing star formation. As a result , they consist mainly aging stars.

### Dwarf Galaxies

A dwarf galaxy is a small galaxy composed of about 1000 up to several billion stars, They have low luminosity and low mass and small in size. They have low surface brightness, so they are



Figure 4.8: Barred Galaxy



Figure 4.9: Lenticular Galaxy

hard to find .Majority of galaxies are dwarfs. Dwarf galaxies may be remnants of galaxy formation process, which is relatively simple systems, not merger product. Dwarf galaxies are currently being cannibalized by larger galaxies.

### 4.3 Galactic Evolution

#### Dynamical Friction

In astrophysics, dynamical friction or Chandrasekhar friction, sometimes called gravitational drag, is loss of momentum and kinetics energy of moving bodies through gravitational interaction with surrounding matter in space. When galaxies interact through collision, dynamical friction between stars causes matter to sink toward the centre of the galaxy and for the orbits of stars to be randomized. This process is called violent relaxation and can change two spiral galaxies into one larger elliptical



Figure 4.10: dwarf galaxies compared to milky way

galaxy.

### Galaxy Formation

Galaxies are collection of stars, gas, dust and dark matter held together by gravity. Their appearance and composition are shaped over billions of years by interaction with groups of stars and other galaxies. Using supercomputers , scientists can look back in time and stimulate how a galaxy may have formed in the early universe and grown into what we see today. Galaxies are thought to begin as small clouds of stars and dust swirling through space. As other clouds get close, gravity sends these objects careening into one another and knits them into large spinning packs. Subsequent collisions can sling material toward a galaxy’s outskirts, creating extensive spiral arms filled with colonies of stars.

## 4.4 Galaxy Merger and Interaction

Interacting galaxies are galaxies whose gravitational fields results in a disturbance of one another .One type of interaction is galaxy collision which may result to galaxies merger if the colliding galaxies do not have enough momentum to continue travelling after the collision.

About 4.5 billion years from now collision between Milky Way and Andromeda will result in galaxies merger and product has been nicknamed as Milkomeda or Milkdromeda. Interesting question is that what happens to the stars of two colliding galaxies ? Do they also collide? No, it is even very less probable that even two stars from the colliding galaxies, collide . They simply pass between the gaps which are very large compared to them.



Figure 4.11: Interacting galaxies



Figure 4.12: Merged galaxies



## 4.5 Intergalactic medium

The intergalactic medium is the hot, X-ray emitting gas that covers the space between galaxies. It has temperature of million of degrees K and density very low( order of  $10^{-27} \text{ Kg}/m^3$ ). Originally it was assumed that the intergalactic medium was composed entirely of primordial hydrogen and helium left over from the Big Bang. However, in the 1970s, X-ray observations revealed large quantities of metals mixed in with the hydrogen and helium. These metals could only have been made by stars within the galaxies, and somehow later ejected into intergalactic space.

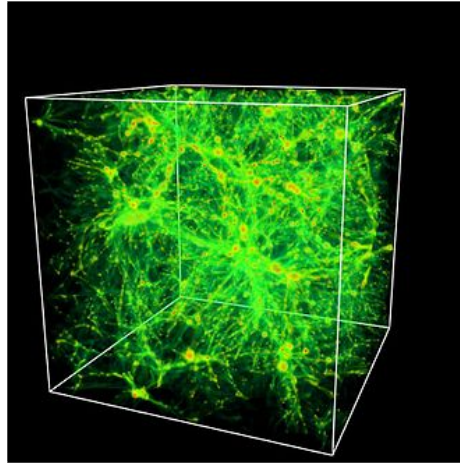


Figure 4.13: Computer simulation of distribution of warm intergalactic gas  
(Image credit : wikipedia.org)

A normal question arises in our mind that 'Why do we need to study IGM?' Following points answer this question:

- More familiar ordinary matter accounts for a small fraction of the mass of the Universe
- About 50 percent of ordinary matter has yet to be accounted for in the present-day Universe. It is "hidden" (or missing) in the intergalactic material
- IGM provides raw materials to build galaxies, stars, planets etc.

IGM gas do not emit appreciably due to its low density but it do absorb radiation coming from a distant background source so only way to detect IGM is through absorption lines imprinted on the spectra of background sources

### Circumgalactic medium

Circumgalactic medium (CGM) is a halo of gas surrounding galaxies that is diffuse, and nearly invisible. Current thinking is that the CGM is an important source of star-forming material, and that it regulates a galaxy's gas supply .How galaxies acquire, eject, and recycle their gas are core issues in galaxy evolution. The CGM is a main venue for these flows: it is potentially the galactic fuel tank, waste dump, and recycling center all at the same time

## 4.6 Galaxy scaling laws

These scaling laws reflects the way in which baryons populate, cool, and settle at the centre of their host dark matter halos ; the angular momentum they retain in the assembly process; as well as the

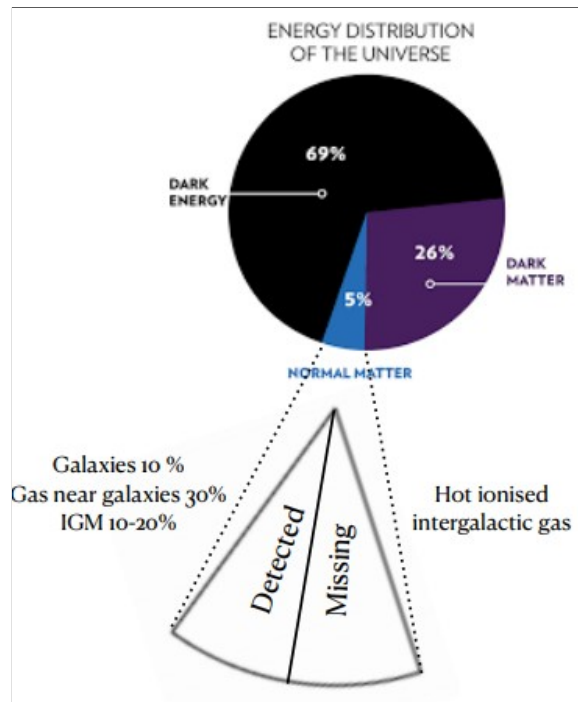


Figure 4.14: Mass/Energy budget of the Universe(Image credit : astronomyonline.org)

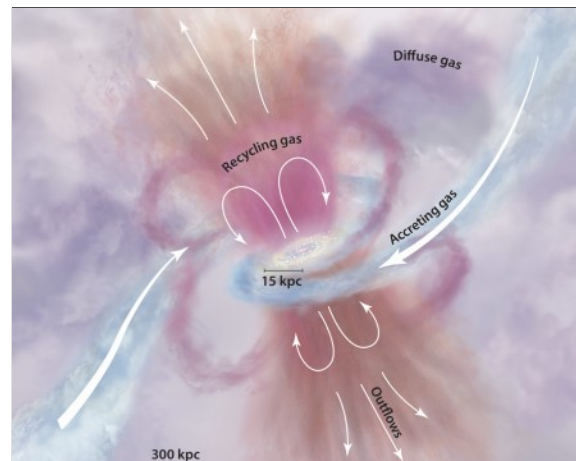


Figure 4.15: A cartoon view of the CGM. The galaxy's red central bulge and blue gaseous disk are fed by filamentary accretion from the IGM (blue). Outflows emerge from the disk in pink and orange, while gas that was previously ejected is recycling.

radial distribution and mass scalings of the dark matters halos.They provides a quantitative means of examining physical properties of galaxies and their systematics.

### The Tully –Fisher Relation

It is a correlation of luminosity vs rotational speed relation for spirals:

$L \approx V^a$ ,  $a = 4$ , varies with wavelength scatters nearly 10 percent at best, better in the redder bands.

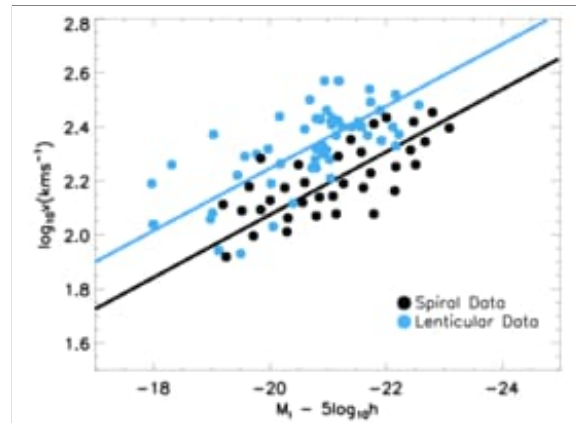


Figure 4.16: Tully –Fisher Relation

TFR is important because it connects a property of the dark halo—the maximum circular speed—with the product of the net integrated star formation history, i.e., the luminosity of the disk. We use TFR to measure relative distances to spiral galaxies.

### Scaling relation for Ellipticals

Many fundamental properties of ellipticals are connected through bivariate scaling relations  $R \approx a^{1.4} I^{-0.8}$ , where  $R$  is the radius,  $I$ : mean surface brightness,  $a$ : velocity dispersion

## 4.7 Milky Way

The Milky Way is the galaxy that includes our solar system. All the stars that we see in night sky are in it. It is a barred spiral galaxy in Virgo supercluster, barred spiral galaxies contains a bar across its central region and have two major arms, Milky way also has two minor arms and two small spurs, one of which known as Orion contain Sun and Solar system. Milky way includes 100-400 billion stars which forms a large disk of diameter 100,000-200,000ly. We get to know the shape of milky way from the bright band of stars that stretch across the sky (which appears as milky band). It is a constantly rotating galaxy so arms (which contain Sun and Solar system) are also moving through space. At the centre of galaxy is the [galactic bulge](#) and at the very center is supermassive black hole which is constantly swallowing dust, gas and nearby stars around it. Most of the galaxies are supposed to have black hole at their center

### Galactic centre of milky way

Observations of the centre of our Galaxy pose a particular challenge. This is because the abundance of gas and dust in the galactic plane results in more than 30 magnitude of extinction at visible wavelengths. Located only 30pc above the midplane and 8kpc from the centre, the line of sight from the sun to the centre traverse nearly the maximum possible amount of interstellar material. There are around 10 million stars within one parsec of the galactic centre, dominated by red giants, with

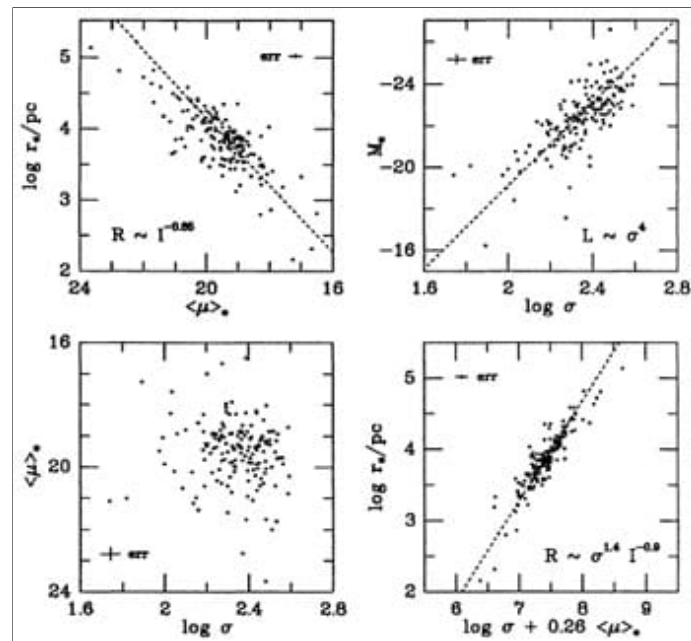


Figure 4.17: Scaling law for Elliptical Galaxies

a significant population of massive supergiants and Wolf-Rayet stars from star formation region around 1 million year ago.

### Some fact about galaxies

1. First galaxy was formed about 1 billion year after the Big Bang which is about 13 to 14 billion years from now.
2. Galaxies come in irregular shapes too, including many dwarf galaxies. These galaxies, the smallest in the universe, contain a few hundred or a few thousand stars (compared with 100 billion stars in the Milky Way.)
3. Most galaxies have a black hole at the centre, and astronomers have founds the mass is consistently about 1/1000th the mass of the host galaxy.
4. Dark matter asides, galaxies are mostly empty space. If the stars within galaxies were shrunk to the size of oranges, they would be separated by 4,800 kilometers.
5. Every galaxy have dust produced by stars, the dust causes light to look redder than it really is when observed visually, which can make it difficult for astronomers studying properties of stars.

### Intergalactic travel

Intergalactic travel is the hypothetical crewed or uncrewed travel between galaxy. Due to the enormous distance between the Milky Way and even its closest neighbour, any such venture would far more technologically demanding than interstellar travel. The technology required travel between galaxies is far beyond humanity's present capabilities, and currently only the subject of speculation, hypothesis, and science fiction. However, theoretically speaking, there is nothing to conclusively indicate that intergalactic travel is impossible.

**Difficulties**

Due to the distance involved, any serious attempt to travel between galaxies would require methods of propulsion far beyond what is currently thought possible in order to bring a large craft close to the speed of light. It would be a journey of millions of earth years via conventional flight.

**Possible methods in theory**

1. Hyper velocity Stars
2. Artificially propelling a star
3. Time dilation
4. Possible faster than light methods

But these methods are just theories for now , we did not even cross our solar system yet. But there is no doubt human will achieve that one day.

“It always seems impossible until it’s done” - Nelson Mandela

**4.8 Links you should check out**

1. Galaxy Merger
2. Type of Galaxies
3. Is Interstellar Travel possible
4. Milky Way Galaxy

## 5. Stellar Evolution

### 5.1 Introduction to Stellar Evolution

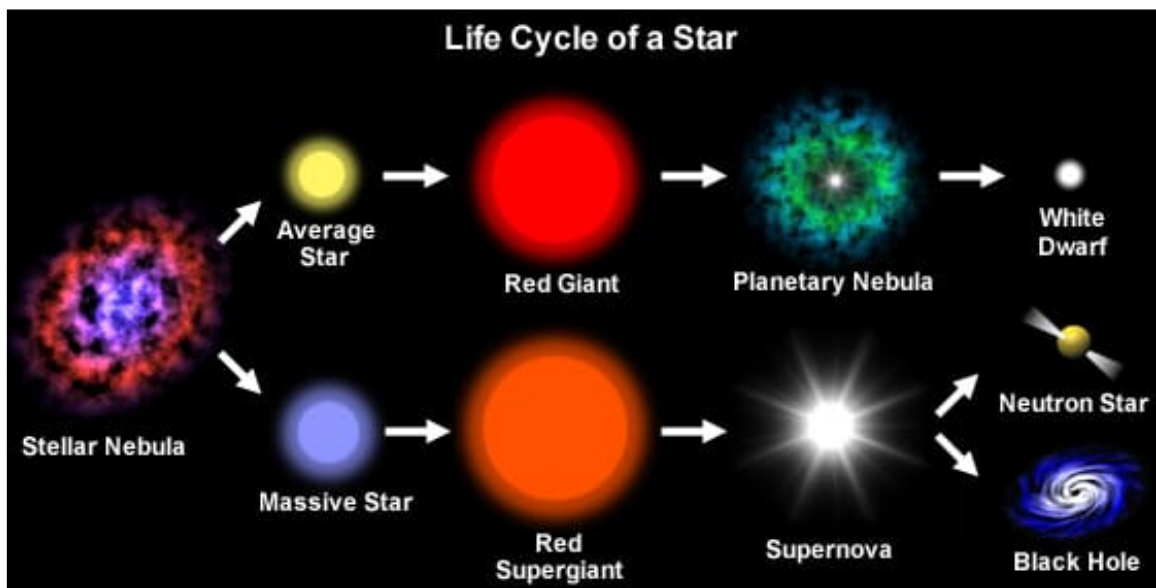


Figure 5.1: Life cycle of a star

When discussing the structure of the Sun, we mentioned in passing that the two most important characteristics governing the properties of a star were its initial mass and its chemical composition. From observations of the orbital motions of binary stars, we know that the lightest ordinary stars have somewhat less than a tenth of a solar mass; the heaviest, somewhat greater than fifty solar masses. We understand this result theoretically in the following way. Gaseous bodies less than about 0.08  $M_{\odot}$ , do not possess enough self-gravity to compress their central regions to sufficiently high temperatures to ignite the nuclear fusion of hydrogen; so, they cannot shine with starlight produced

by nuclear reactions. Such bodies—like Jupiter—are not called stars. Bodies greater than about 60  $M_{\odot}$ , on the other hand, possess so much self-gravity that their interiors are compressed to very high temperatures. Under such conditions, radiation pressure begins to dominate greatly matter pressure. Stars evidently cannot exist stably or cannot form in the first place, with such high masses.

To deduce the initial chemical composition of stars the most direct technique was initiated by Payne (later Payne-Gaposchkin) and consists of analyzing the line spectrum of the radiation which comes from the photosphere of a star. One then assumes that the photosphere is uncontaminated by nuclear processing in the interior, so that the photospheric composition is basically primitive. The half-lives of all the isotopes of technetium are less than a few million years, quite short by stellar standards. Consequently, technetium at least must have recently been synthesized in the interiors of these stars in question, then brought to the surface by some process or another. Other stars, called R and N stars, show anomalously high abundances of carbon in their spectra. However, stars with peculiar chemical abundances in their photospheres constitute a definite minority of all stars.

From spectroscopic studies of normal stars and their surroundings, it has been learned that most stars initially contain about 70 percent hydrogen by weight and about 28 percent helium. Stars which are relatively rich in heavy elements—such as our Sun—are called population I stars; stars which are relatively poor in heavy elements—such as globular-cluster stars—are called population II stars. No star with zero heavy-element abundance has ever been found; however, some astronomers have theorized that such stars do exist and have dubbed this hypothetical earliest generation of stars, population III. The main lesson to be learned from the study of chemical composition of the stars is that stars evidently start their lives predominantly made of hydrogen and helium. This predominance of hydrogen and helium in the present universe suggests that the universe started under conditions of extremely high temperature. Under such conditions, matter prefers more particles, i.e., more simple elements like hydrogen and helium.

In any case, we learn from the above discussion that the Sun is quite a mediocre star, in terms of both its chemical composition and its mass. It is reasonably rich in heavy elements, but not as rich as extreme population I stars. It also has a lowish mass, but even that is quite normal, since the Galaxy turns out to have many more stars of low mass than stars of high mass. We shall soon see that the age of the Sun is also quite mediocre.

## 5.2 Theoretical H-R Diagram

The theoretical H-R diagram is a plot of the luminosity  $L$  of a star versus its effective temperature  $T$ , (Fig 5.2 on next page). Most stars when plotted in such a diagram are found to be located on a diagonal band called the main sequence. Stars on the main sequence are essentially chemically homogeneous and are burning hydrogen into helium in their cores. The stars can quietly and steadily shine for the greatest period of their luminous lifetime. Consequently, most easily observed stars for which we can derive  $L$  and  $T$ , observationally lie on the main sequence.

## 5.3 Properties of Stars on the Main Sequence

What makes one star lie at one position on the band, and another star at another position? It turns out that different initial amounts of elements heavier than hydrogen and helium make relatively little difference in the gross properties on the main sequence. The major factor which determines a main-sequence star's position in the H-R diagram is its mass. High-mass stars expend energy much faster than low-mass stars. As Eddington first discussed, the rate at which heat leaks out of stars by

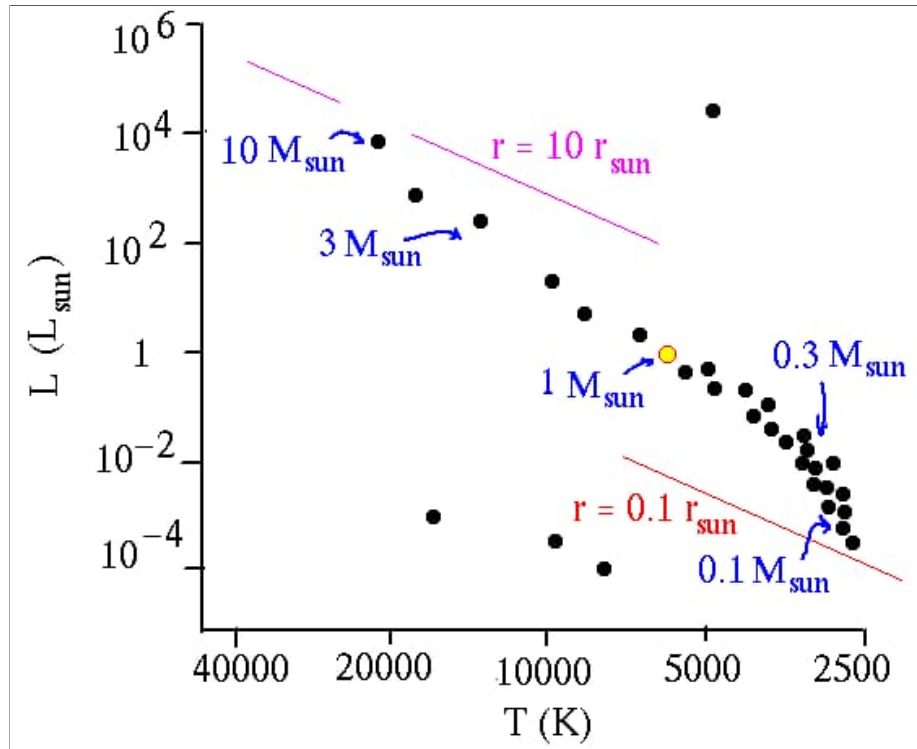


Figure 5.2: The location of the main sequence in the theoretical Hertzsprung-Russell diagram. The points give the theoretical positions of stars of various masses which have just begun their lives as main-sequence stars (the so-called “zero-age main sequence”).

radioactive diffusion yields a luminosity  $L$  which depends roughly on the mass  $M$  to the fourth power. We already showed that the rate of radioactive leakage of photons from the interior of a star was given by:-

$$L = \frac{(4\pi R^3/3)(aT^4)}{3R^2/lc}$$

where  $R$ =Radius of the star,  $T$  = Mean interior temperature,  $a$  = Radiation constant,  $c$ =Speed of light,  $l$ =mean free path for the “random walk” of the photon To derive a mass-luminosity relationship, we wish to express  $T$  and  $l$  in terms of  $M$  and  $R$ . Moreover, for our purposes here, we are interested only in proportional relationships. It turns out that the opacity in main sequence stars is such that the mean free path  $l$  works out to be

$$l \propto T^{3.5}/\rho^2 \quad \text{for stars with low to medium mass} \quad (5.1)$$

$$l \propto 1/\rho \quad \text{for stars with high and very high mass} \quad (5.2)$$

where  $\rho$  is the mean density. The reason for these dependencies is briefly the following. At very high temperatures, all the electrons are stripped from atoms, and the primary source of opacity is the scattering of X-rays from free electrons. This scattering depends only on the number of electrons per unit volume; i.e., the mean free path  $l$  in high-mass stars should be proportional to the reciprocal of



the mass density  $\rho$  (the higher the density, the shorter the mean free path). At lower temperatures, some electrons are still bound to the ions, and these inner-shell electrons contribute most to the X-ray opacity. However, the number of such incompletely ionized contributors goes down if the temperature goes up, and the number rises if the density goes up. The mean free path  $l$  is inversely proportional to the number of opacity contributors, and  $l$  in low-mass stars works out to be  $\propto T^{3.5}/\rho^2$

where  $P$  is the total pressure. In stars with low to high mass,  $P$  can be taken to be the gas pressure, but in stars with very high mass, radiation pressure dominates. Argue therefore,

$$P \propto \rho T \quad \text{for stars with low to high mass} \quad (5.3)$$

$$P \propto T^4 \quad \text{for stars with very high mass} \quad (5.4)$$

Use the above formulae now to show the results:

$$L \propto M^{5.5}/R^{0.5} \quad \text{for stars with low to high mass} \quad (5.5)$$

$$L \propto M^3 \quad \text{for stars with high mass} \quad (5.6)$$

$$L \propto M \quad \text{for stars with very high mass} \quad (5.7)$$

Since stars with very high mass are extremely rare, argue that  $L \propto M^4$  gives a good compromise for the entire range of masses on the main sequence.

since the energy stored and luminosity both are proportional to  $M$ , we may say that the lifetime is proportional to  $M^{-3}$ .

The main-sequence lifetimes of the heaviest stars turn out to be virtually independent of  $M$ , and are in the neighbourhood of a few million years. The balance of energy release by hydrogen burning in the core and energy flow to the surface leads to a radius  $R$  on the the sequence which is roughly proportional to the mass. Thus, a 10M. star is roughly ten times the size of the Sun. If we combine the dependency of radius and luminosity with mass and the equation for calculating luminosity , we can derive

$$T_e \propto M^{1/2}$$

Thus, high-mass stars have hotter surfaces and higher luminosities than low-mass stars on the main sequence.

Stars of a given mass have their smallest sizes as normal stars when they are on the main sequence; thus, main-sequence stars are also called dwarfs. Main sequence dwarfs are not to be confused with white dwarfs, which are not normal stars, and which are quite a bit smaller than their main-sequence counterparts of the same mass. White dwarfs of a given mass have the same radii, but they may have different locations in the H-R diagram if they have different effective temperatures.

## 5.4 Evolution of Low-Mass Stars

### Ascending the Giant Branch

As the core contracts, it heats itself up as well as the layers just above it. At the new higher temperatures, hydrogen can begin to burn in a shell just outside the hydrogen-exhausted core.

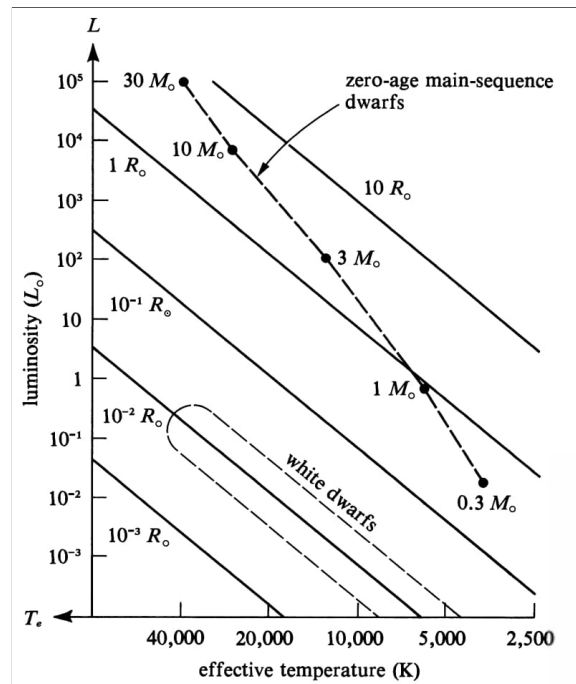


Figure 5.3: Main-sequence dwarfs and white dwarfs. The solid diagonal lines give loci of constant radii.

However, the helium core itself still has no nuclear-energy generation, and as it continues to lose heat to the cooler overlying layers, it must continue to contract. The shrinkage of the core accompanied by the addition of more mass makes the gravity at the border of the core stronger and stronger, so the gravitational field felt by the hydrogen burning shell becomes stronger and stronger. But the pressure in the shell equals the weight of a column of material of unit area above it. This pressure must therefore try to increase to counterbalance the increasing gravity of the core. The pressure of the ordinary gas in the shell can be increased, in accordance to the perfect-gas law, either by raising the density or by raising the temperature. In fact, both occur, and both increase the rate of hydrogen burning in the shell. The difference between the luminosity generated in the shell source and that leaving the surface goes into heating up the intermediate layers, causing them to expand. This expansion increases the total radius  $R$ ; given a nearly constant value for the surface luminosity  $L$ , there must be a decrease of the effective temperature  $T$ , in accordance with the relation of luminosity with radius and temperature of an object.

The immediate post-main-sequence evolution of a radioactive star therefore moves the star's position more-or-less horizontally to the right in the H-R diagram, turning the dwarf star into a subgiant. The cooling and expanding surface layers cause the star to turn red in outward appearance. Hayashi and his co-workers pointed out that the ability of the photospheric layers to prevent the free streaming of photons drops rapidly with decreasing temperatures. This ease for photon streaming in turn leads to a minimum temperature below which  $T$ , is prevented from falling. The existence of such a temperature barrier forces the evolutionary tracks of low-mass stars in the H-R diagram, sooner or later, to travel almost vertically upward, turning the red subgiant into a red giant. The accompanying increase in the amount of shell luminosity which makes its way to the surface is too much for radioactive diffusion to carry outward stably, and the entire envelope of the red giant

becomes convective.

Let us try to understand Hayashi's important result qualitatively. A stellar photosphere is defined to be that level (a) where photons stop "walking" and start "flying," and (b) where the gas temperature  $T$  approximately equals the effective temperature  $T_e$ . Argue that condition (a) implies that the mean free path of the photons,  $l$ , must be comparable to the thickness  $H$  of the photosphere. Argue that hydrostatic equilibrium requires the pressure  $P$  to balance the weight  $pH$ . Use the perfect-gas law to derive now a relationship between  $l$  and  $T$ . In a cool stellar atmosphere,  $l$  is very sensitive to  $T$  and relatively insensitive to  $p$ . Show that this requires  $T$  to have almost a fixed value throughout a wide range of photospheric densities  $p$ . Thus, show that given  $R$ , the luminosity  $L$  must therefore accord with this value of  $T$ , because of condition (b). If this required  $L$  exceeds the value which can be carried stably by radioactive diffusion in the envelope, argue that the envelope will become convective. Meanwhile, the core continues to contract, and in a low-mass star, the free electrons become so tightly packed that they become degenerate.

### The Helium Flash and Descent to the Horizontal Branch

The ignition of helium in the core of a low-mass star, however, occurs under degenerate conditions; So, it lacks the safety-valve feature which characterizes core hydrogen burning on the main sequence. Here, the pressure increases primarily because of degeneracy effects, not because of thermal motions; So, an increase of the core temperature leads to an overproduction of nuclear energy without a compensating pressure increase and a compensating expansion.

Higher temperatures  $\rightarrow$  more nuclear energy  $\rightarrow$  even higher temperatures, etc.

Therefore, helium burning turns on in low-mass stars with a "flash," as was first suggested by Mestel and verified in detailed calculations by Schwarzschild and Harm. So much energy is released in the "flash" that the core's temperature rises enough to remove the degeneracy. Normal thermal pressure then dominates over electron degeneracy pressure, and the core expands. This expansion lowers the border gravity of the core, which weakens the hydrogen-shell source.

After the helium flash is completed, the core contains an ordinary (i.e., non degenerate) helium plasma which is stably fusing helium into carbon. Surrounding this core is a hydrogen-burning shell, whose strength depends on the mass of the overlying envelope. This state of core-helium burning and shell-hydrogen burning is called the horizontal branch. The exact location of a horizontal-branch star in the theoretical H-R diagram depends not only on its initial mass and chemical composition on the main sequence, but also on the amount of envelope mass lost by the star as it ascended the red-giant branch.

For a group of stars which start on the lower main sequence with similar initial masses and chemical compositions, the stars which lose more mass on the red-giant branch end up on the horizontal branch with smaller envelope masses and, therefore, weaker shell sources in addition to the core source. A horizontal branch star which had lost all its envelope mass would be a chemically homogeneous helium star burning helium into carbon at its centre. Such a state is often called the "helium main sequence" by analogy with the usual (hydrogen) main sequence. Most horizontal-branch stars, however, have a finite envelope mass on top of such a helium-burning core, and the hydrogen-burning shell associated with the weight of this envelope keeps the envelope relatively distended. Thus, true horizontal branch stars tend to have slightly higher luminosities than a "helium-main-sequence" star of the same core mass, as well as appreciably lower effective temperatures. If we started with a group of stars, therefore, with similar initial masses and chemical compositions, and if this group suffered varying amounts of envelope-mass loss ascending the

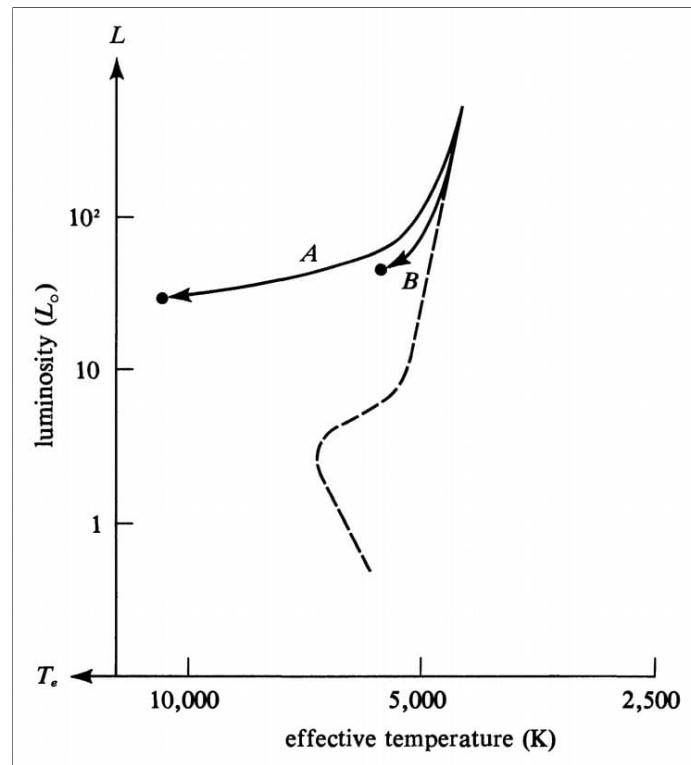


Figure 5.4: Descent of a low-mass star with poor heavy-element abundances (Population II star) from the tip of the red-giant branch to the horizontal branch. Track A corresponds to a star which suffered a relatively large loss of mass during the red giant phase of stellar evolution. Track B corresponds to a star which suffered relatively little loss of mass.

red-giant branch, we should expect them to end on the horizontal branch with nearly the same luminosities but with different effective temperatures.

To deduce the approximate location in the H-R diagram of a “helium main-sequence star” of  $0.5M_{\odot}$ , For a chemically homogeneous star of low mass which has a radioactive interior, we showed that the luminosity  $L$  satisfied:

$$L \propto RT^{7.5}/p^2$$

with  $R$  equal to the radius,  $T$  the average internal temperature, and  $p$  the average mass density. If ordinary gas pressure dominates,  $T$  is related to the pressure  $P$  and the number density  $n$  by the formula

$$L \propto P/n$$

The number density  $n$  and the mass density are related via  $p = mn$ , where  $m$  is the mean mass of all the constituent particles. Let  $X$  = the mass fraction of hydrogen, where  $n_y$ , is the number density of hydrogen nuclei and let  $Y$  = the mass fraction of helium, where  $n_{He}$ , is the number density of helium nuclei. In the interior of the star, hydrogen and helium are completely ionized. Since each hydrogen atom contributes two particles (a hydrogen nucleus and an electron), and each helium atom contributes three particles (a helium nucleus and two electrons). With  $Y=1-X$  (extreme Population

If star which has virtually no heavy elements), show that the mean mass  $m$  is given by

$$m = (4/5X + 3)m_p$$

Retrace now the arguments of above given equations to show that

$$T \propto Mm/R$$

### Ascending the Asymptotic Giant Branch

The core must contract when helium in the core of a horizontal branch star is exhausted, which increases the pressure and temperature of the overlying layers. Thus, helium ignites in a shell just outside the core, and hydrogen burns in a shell outside of that. The star is now in a double-shell-burning stage. The mass of the inert carbon-oxygen core continues to increase, and it continues to contract just as the helium core did when the star ascended the red-giant branch for the first time. Indeed, the energy generation in the (two) shell sources must proceed at an ever-increasing pace just as before, and the rapidly increasing luminosity must distend the overlying envelope just as before. Thus, the star must ascend the red-giant branch again, and the double-shell source phase is also known as the asymptotic giant branch. Eventually, the shrinkage of the core again causes the free electrons to become degenerate. Stars at the end of the double-shell-burning phase may become red supergiants. At such tremendous rates of expenditures of energy, the star cannot live much longer. The origin of this instability is very different from the “helium flash” discussed earlier. There, an initial overproduction of nuclear energy leads to a runaway because of the degeneracy of the nuclear-burning region. Here, an initial overproduction of nuclear energy also leads to a thermal runaway, but for an entirely different reason. Here, the nuclear burning region is non degenerate, but it is a spatially thin shell. Thus, with the input of excess nuclear energy, the layer can and will expand. But the expansion of a thin shell does little to relieve the weight of the overlying material; this material is lifted only a little. Thus, the weight hardly changes, and therefore the pressure that the thin shell must maintain to offset this weight also hardly changes.

### Planetary nebulae and white dwarfs

Among the many promising mechanisms which have been considered is the suggestion that small specks of dust may form in the cool atmospheres and be driven out subsequently by the radiation pressure of the star. Quantitative calculations, unfortunately, are difficult. Observations indicate that stars that originally had less than about six solar masses seem to lose so much mass during such high-luminosity stages that they become (perhaps periodically) planetary nebulae illuminated by a hot central core. This hot central core is presumably an incipient white dwarf, with mass necessarily below the Chandrasekhar limit  $1.4M_{\odot}$ . From the central-star stage of planetary nebulae, the exposed core burns out its hydrogen and helium shells, loses its extended envelope, and descends the H-R diagram to enter the region occupied by white dwarfs proper. Figure below summarizes the complete evolution of a low-mass star from the main sequence to a carbon-oxygen white dwarf. The final approach to a white dwarf from an asymptotic giant star is shown in dashed lines, to emphasize that the theory is incomplete for these late stages of stellar evolution.

### Approach to the Iron Catastrophe

In high-mass stars, core-hydrogen exhaustion, helium core contraction, and shell-hydrogen ignition occur pretty much as for low-mass stars, with only minor differences. The main difference is that in

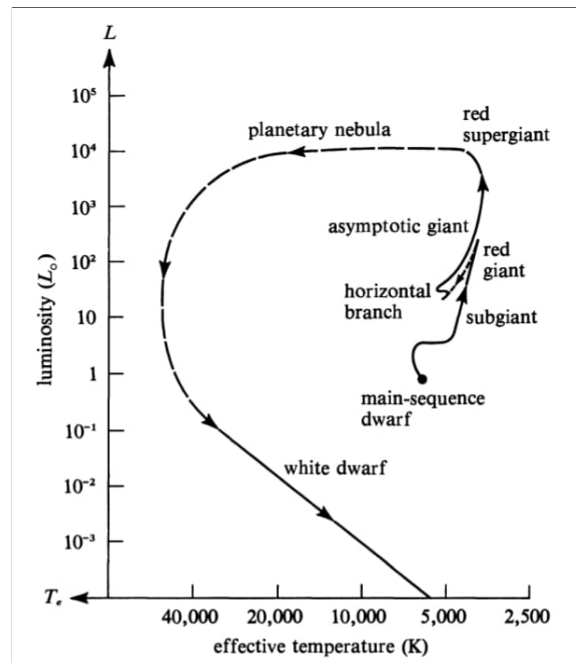


Figure 5.5: The complete evolution of a low-mass star from the main sequence to a white dwarf. The track from the asymptotic giant branch to a white dwarf (via a planetary nebula) is uncertain and is shown as a dashed curve.

stars with initially more than  $2.25M_{\odot}$ , core-helium ignition occurs before the core has contracted very far. Helium ignites in the cores of these higher-mass stars under non degenerate conditions, and there is no helium flash. During helium core burning, hydrogen-shell burning continues at about the same rate as before core ignition. During core contraction, the star moves generally to the right (lower  $T_e$ ) in the H-R diagram. After core ignition, the star moves generally to the left (higher  $T_e$ ). In high-mass stars, these rightward (core exhaustion) and leftward (core ignition) excursions occur with only a slight systematic increase of the luminosity; hence, the evolutionary tracks of high mass stars occur virtually horizontally in the H-R diagram. In very-high-mass stars, the nuclear evolution in the central regions of the star occurs so quickly that the outer layers have no time to respond to the successive rounds of core exhaustion and core ignition, and there is only a relatively steady drift to the right of the H-R diagram before the star arrives at the presupernova state. In any case, helium-core burning and hydrogen-shell burning is followed by core-helium exhaustion. The carbon-oxygen core then contracts, and ignites a helium shell source below the hydrogen-shell source, as before. In its turn, the carbon-oxygen core will also ignite. Carbon burning has a very high temperature sensitivity and a relatively large energy release per gram of fuel.

In stars whose original mass was higher than about  $10M_{\odot}$ , the carbon will ignite at several hundred million K, before electron degeneracy becomes important. All stars of sufficiently high mass will therefore evolve by successively using up one round of fuel in the core, undergoing core contraction, achieving core ignition of previous ash into new fuel, etc. In the simplest models (proposed first by Fowler and Hoyle, and calculated by Arnett and by Paczynski), the core will be surrounded by more and more shell sources, much as an onion is surrounded by many layers. The cycle of turning ash into new fuel proceeds faster and faster as the now degenerate core approaches closer and closer to

the Chandrasekhar limiting mass. Finally, iron is produced in the core.

## 5.5 Conclusion

Zeldovich and Novikov have made the following intriguing philosophical point about the picture of the formation of a neutron star sketched here. They note that stars begin their lives as a mixture mostly of hydrogen nuclei and their stripped electrons. During a massive star's luminous phase, the protons are combined by a variety of complicated reactions into heavier and heavier elements. The nuclear binding energy released this way ultimately provides entertainment and employment for astronomers. In the end, however, the supernova process serves to undo most of this nuclear evolution. In the end, the core forms a mass of neutrons. Now, the final state, neutrons, contains less nuclear binding energy than the initial state, protons, and electrons.

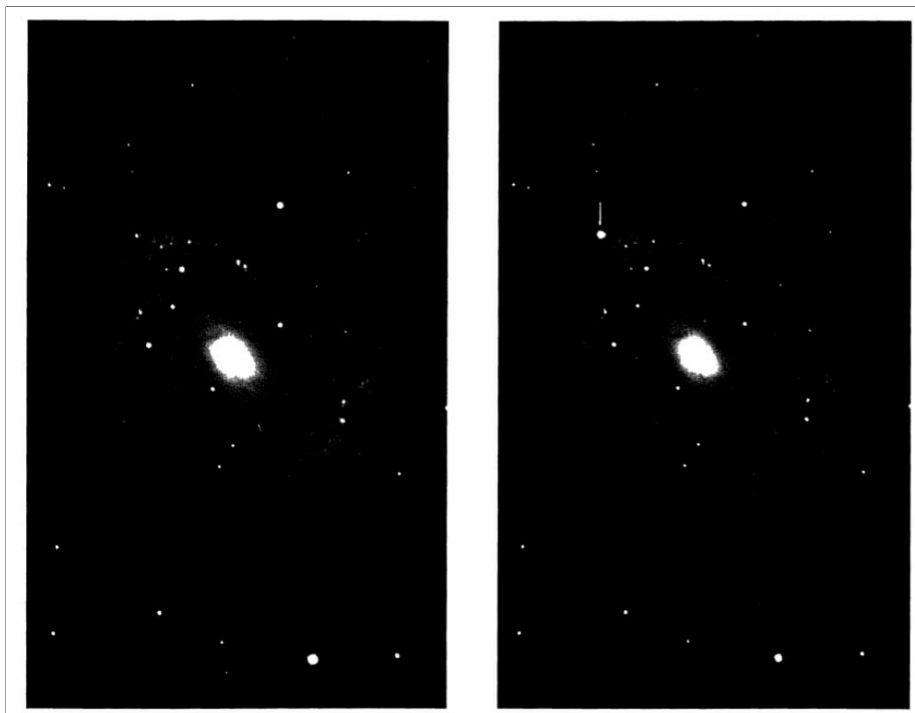


Figure 5.6: A supernova appeared between May 10, 1940, and January 2, 1941, in NGC 4725, a spiral galaxy in Coma Berenices. The earlier photograph on the left shows the galaxy; the later photograph on the right shows that a supernova had exploded during the interim in one of the spiral arms.



## 6. Cosmology and Early Universe

### 6.1 Cosmology

The Hubble's law direct implication was that we live in an rapidly expanding universe and we need to be at the centre of this expansion, but so has everything else too! Also, how gravity, an attractive force at all distances, is allowing this expansion! Firstly, we will attempt to understand and solve these problems from the point of view of Newtonian mechanics and after that we make use of the insights provided by the general relativity or the modern ideas of particle physics.

#### 6.1.1 Newtonian Cosmology

##### The Olbers' Paradox

Newton believed in an infinite static universe filled with a uniform scattering of stars. This uniformity was necessary for a stable universe otherwise due to the attractive gravitational force it would collapse inwards.

However, the flaw in this model was first pointed out by Edmund Halley and then subsequently by Heinrich Olbers. Olbers argued that if we live in an infinite, transparent universe filled with stars, then in any direction one looks in the night sky, one's line of sight will fall on the surface of a star and hence the sky shouldn't be dark at all during night. A possible answer to this paradox was that space is not transparent. However, if there was any obscuring matter hiding the stars beyond, it would be heated up by the starlight until it glowed as brightly as a stellar surface.

The solution of this paradox came from Edgar Allan Poe who proposed that because light has a finite speed and the universe is not infinitely old, the light from the most distant sources has not yet arrived.

##### The Cosmological Principle

The cosmological principle is the assumption that the spatial distribution of matter in the universe is homogeneous and isotropic when viewed on a large enough scale. It has been argued that Hubble's law is a natural outcome of the Cosmological Principle itself. We can argue that this definitely is not



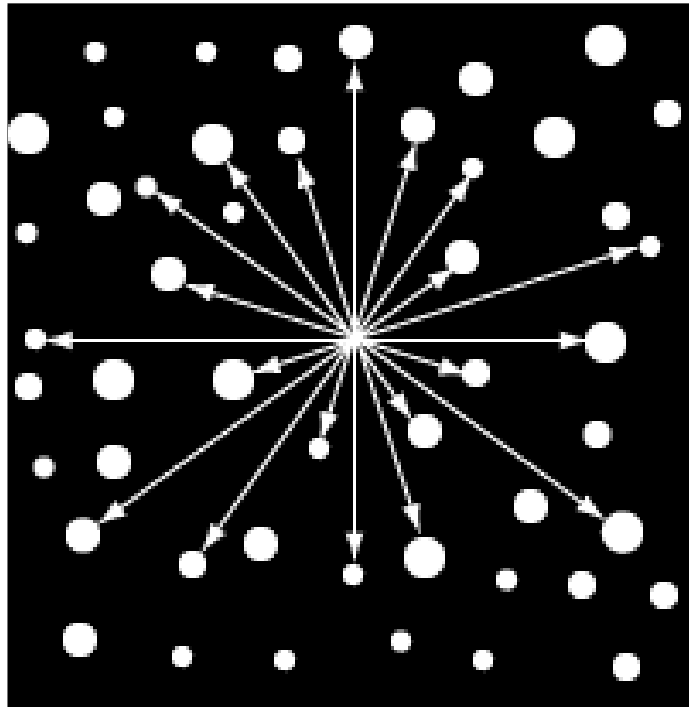


Figure 6.1: Olber argued that an infinite universe will have stars at every possible line of sight

true even at the scale of millions of light years when we see huge cluster of galaxies. However, the principle takes its large scale to be billions of light years (really large!).

It follows from the Cosmological Principle that the rate of expansion is the same throughout the universe. A useful analogy to understand this model is a rising cake or an inflating balloon model.

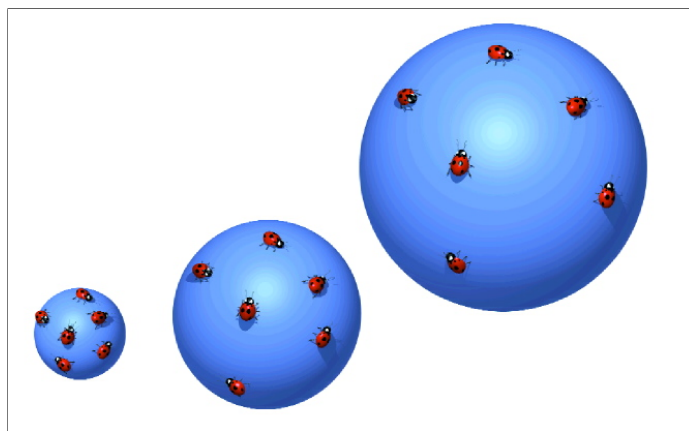


Figure 6.2: The points on balloon farther from each other recede faster from each other. This is a consequence of uniform rate of expansion of the balloon in every part of its surface.

Building up on the Cosmological principle, let's try to analyse a perfectly uniform universe by Newtonian principles. If the universe is completely uniform then the gravitational field ( $g$ ) should be zero everywhere (due to linear superposition of equal contribution from all directions.) However, this

lands us into a problem as we apply Gauss' law. For any arbitrary volume  $V$  containing mass  $M$ ,  $g=0$  yields,

$$4\pi GM = 0 \quad (6.1)$$

However, we know that this conclusion is absurd because  $M$  cannot be zero as the universe is not empty!

### Bound vs Unbound universe

To counter the absurdity which presented itself in the previous section, Garret Birkhoff gave **Birkhoff's rule**. He stated that we must rectify the situation by replacing the Gauss' rule by the following rule. The velocity of a galaxy located at distance  $r$  from the observer is only influenced by all the matter which lies inside a sphere of radius  $r$  centered around the observer. If we do accept

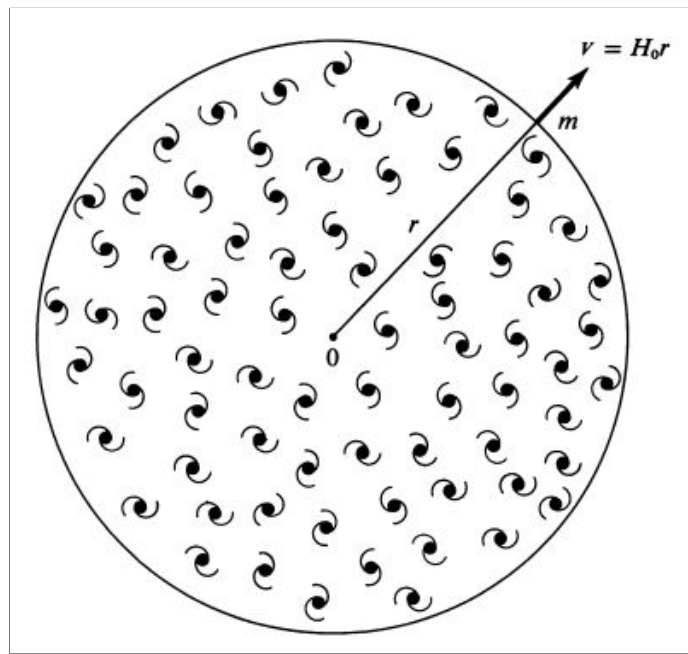


Figure 6.3: Illustration of Birkhoff's rule. The motion of a galaxy  $m$  appears to an observer  $O$  to be only affected by the mass inside the sphere with radius  $r$ .

this rule, then we can calculate the deceleration of the universe due to gravitation. The total energy of a moving galaxy is given as

$$E = \frac{1}{2}mv^2 - GMm/r \quad (6.2)$$

where  $v=H_0r$ . Now if  $E<0$ , then the galaxy will fall back to  $O$ (it is bound), otherwise it will recede forever. The critical case  $E=0$  is met when the average density is

$$\rho_{m0} = 3H_0^2 / 8\pi G \quad (6.3)$$

If the present mass density equals  $\rho_{m0}$  then the universe is marginally bound, if it is greater than  $\rho_{m0}$  then it is bound and if less than  $\rho_{m0}$  then unbound.

The ultimate fate of the universe depends on whether it is bound or unbound. An unbound universe will keep on expanding and all the stars will eventually die out leaving a pitch-dark and

empty universe. If the universe is actually bound then someday the recession will come to a halt and then due to gravity, the universe will start collapsing onto itself leading to the **Big Squeeze**, and possibly a cycle of Big bang and Big squeeze again(possibly!).

### 6.1.2 Relativistic Cosmology

Till now, while analysing the universe by Newtonian approach, we came across a lot of absurdities which has somewhere made us realise that a modern approach using relativistic mechanics is needed. The appearance of objects at truly cosmological distances is affected by the curvature of the spacetime through which the light travels on its way to Earth. Before moving on to relativistic models, let's begin our analysis with some simple concepts about spacetime curvature.

#### The spacetime curvature

The principle of equivalence states that the gravitational force felt by an object is equivalent to the pseudo-force experienced by an observer in a non-inertial (accelerated) frame of reference. Now if this principle is taken to be true then since light takes a finite time to traverse a distance, for an observer in the non-inertial frame of reference, light would seem to take a curved path. Equivalently, if the observer is in the gravitational field, he may account that the path of light bends due to gravity.

Hence, Einstein predicted that light must bend around massive objects. His theory was verified when Eddington in 1919 verified the presence of Gravitational lensing during solar eclipse.

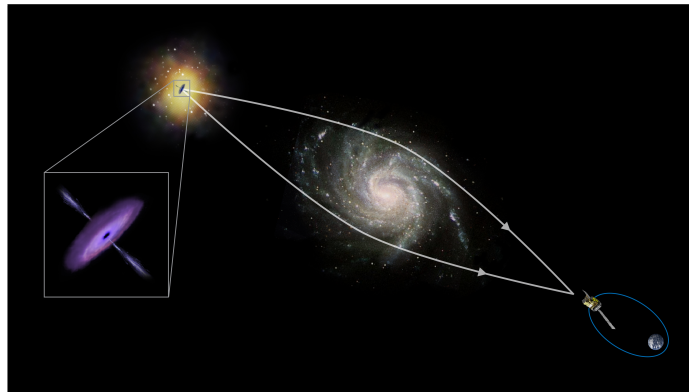


Figure 6.4: Gravitational lensing (Light bends around the massive galaxy and reaches the observer at earth which otherwise would have diverged out)

Instead of calling it an effect of gravitational force, it is termed as an geometrical effect due to the curvature of spacetime itself and light takes the shortest path always between the two points in this curved spacetime.

#### The story of Cosmological constant

In 1915, Einstein published his equations of General Relativity. This theory was aimed at improving upon the Newton's law of Gravitation and hoped to clear out all the cosmological paradoxes which arose at its application at the cosmic scale.

On solving the equations gave a dynamic universe as solution whose space coordinates were dependent on time. Einstein saw this as a fault in the model as he believed in a static universe. That is why he introduced the cosmological constants in his equation. However, not far later, Hubble,

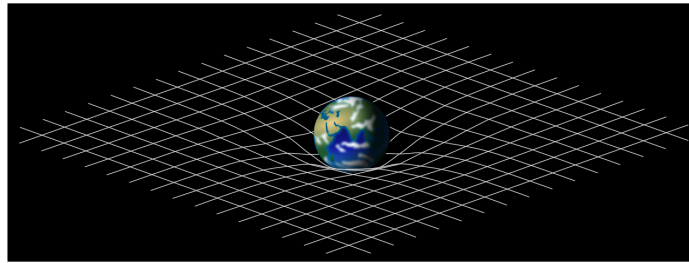


Figure 6.5: Depiction of the curved spacetime around earth

through his observations established that the universe is actually expanding and thus not static. This made Einstein realise his mistake.

Einstein finally took into account the theory of an expanding universe and put the cosmological constant in his equations as 0. Together with de Sitter, he proposed the Einstein-de Sitter model.

Today's observations point out that there may be a non zero cosmological constant however that would be 120 orders of magnitude smaller than that of Einstein's. Einstein himself called the cosmological constant as the biggest mistake of his life.

#### **Einstein-de Sitter model**

The Einstein-DeSitter model is a matter dominated Friedmann model with zero curvature ( $k = 0$ ). This model corresponds to a Minkowski universe (zero curvature), in which the universe will continue to expand forever with just the right amount of energy to escape to infinity. It is analogous to launching a rocket. If the rocket is given insufficient energy, it will be pulled back by the Earth. However, if its energy exceeds a certain critical velocity (escape velocity), it will continue into space with ever increasing speed. If it has exactly the escape velocity, it will proceed to escape the Earth with a velocity going to zero as the rocket approaches spatial infinity. The Einstein-DeSitter model corresponds to the universe having exactly the right escape velocity provided by the Big-Bang to escape the pull of gravity due to the matter in the universe. Most of space is empty and the concern is the total energy density.

The critical density depends on the Hubble constant. This means that the density required for a flat universe will change with time, in general, as the universe expands. For the universe to be 'fine-tuned' to this precision is highly improbable; yet, most observations suggest this type of geometry. This paradoxical issue is referred to as the Flatness problem and will lead to one of the claimed triumphs of Inflation theory. Because it is believed that the universe is so close to being flat.

#### **Friedmann-Lemaitre model**

Friedmann derived the Friedmann equations which were compatible with the GTR for any value of the Cosmological constant. There were primarily two sets of solutions that gave rise to closed and open universe as solutions. Lemaitre further expanded on Friedmann's works and created the Friedmann-Lemaitre model of Universe.

On surface, the two classes of the Friedmann-Lemaitre model appear to be analogous to the bound and unbound universes of the Newtonian Cosmology whereas the Einstein-de Sitter model is an analogue of the marginally bound case. However, there is a crucial difference between the two concepts. The Newtonian model assumes a rigid concept of absolute space and absolute time therefore one can mathematically vary the Energy parameter to change the bound universe model to unbound universe model. However, in the relativistic cosmology model they are different in their

structure itself. Till 1980s, the scientists opinion aligned mostly towards the Einstein–de Sitter model

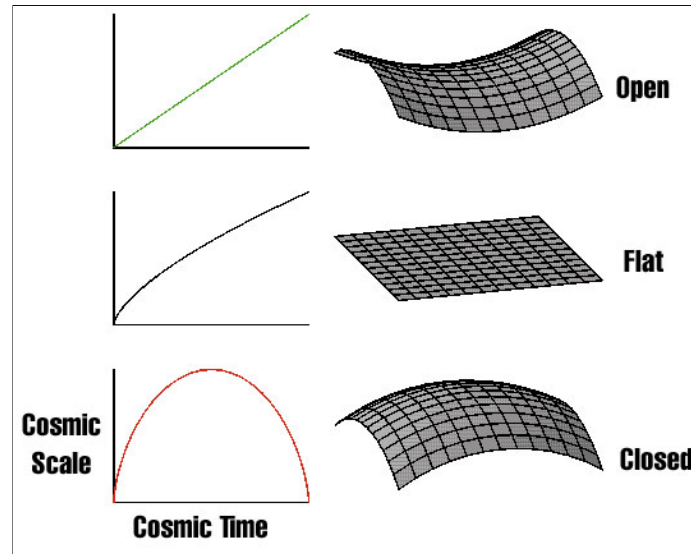


Figure 6.6: The structure of closed and open universes as predicted by Friedmann-Lemaitre model and the flat universe as predicted by the Einstein-de sitter model

after the theory of cosmic inflation predicted that the curvature of the universe should be very close to zero. However, in the 1990s, various observations including galaxy clustering and measurements of the Hubble constant led to increasingly serious problems for this model. Following the discovery of the accelerating universe in 1998, and observations of the cosmic microwave background and galaxy redshift surveys in 2000–2003, it is now generally accepted that dark energy makes up around 70 percent of the present energy density while cold dark matter contributes around 25 percent, as in the modern Lambda-CDM model. The Einstein–de Sitter model remains a good approximation to our universe well after the radiation-dominated era but before dark energy became important.

## 6.2 The Early Universe

This part of the chapter deals with the emergence of structure from the featureless cauldron of the **Big Bang**. Much happened during the universe’s first fraction of a second, and the nature of that earliest environment is still only partially understood. The ideas of modern particle physics that describe these early epochs have also made successful predictions about the types and numbers of elementary particles that exist today. It is to these theories that we turn (with some measure of confidence) in hopes of glimpsing the engines of creation.

### 6.2.1 The Very Early Universe and Inflation

#### Fundamental Particles

According to the **Standard Model** of particle physics, there are three kinds of fundamental (not composite) particles.

- The **leptons** are the charged leptons  $e^\pm$ ,  $\mu^\pm$ , and  $\tau^\pm$ , and the neutrinos  $\nu_e$ ,  $\nu_\mu$ , and  $\nu_\tau$ , together with their antineutrinos. Leptons are **fermions**.

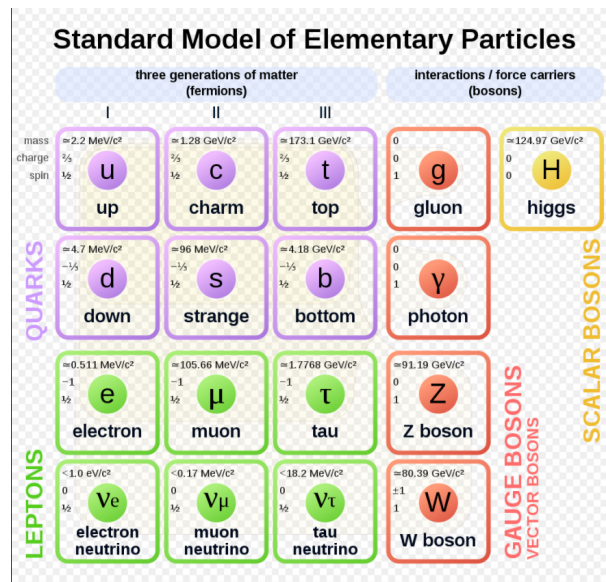


Figure 6.7: Standard Model of Fundamental Particles

- There are six **quarks**: up, down, strange, charm, bottom, and top, along with their antiquarks. Each quark comes in three “colors” (three choices of an internal degree of freedom). Particles made of quarks are called **hadrons**. There are two types of hadrons: **baryons** (made of three quarks) and **mesons** (formed by a quark–antiquark pair). Baryons are fermions, while mesons are bosons.

- The **force-carrying particles** consist of the photon, eight different gluons (particles that mediate the strong interaction and bind quarks together), three vector gauge bosons (W and Z<sup>0</sup>) that mediate the weak interaction, and the scalar Higgs boson (which has yet to be confirmed by experiment). All of these particles are bosons.

Current technology can reproduce the temperatures, energies, and densities that prevailed back to the **quark–hadron transition** at about  $10^{-5}$  s, when a plasma of free quarks and gluons condensed to form hadrons, including the familiar proton and neutron.

### Hot and Cold Dark Matter

Determining the composition of dark matter is one of the greatest challenges facing cosmologists today. Some dark matter may consist of ordinary baryonic matter, although the total amount of **baryonic matter** (both shining and dark) cannot make up more than 4 percent of the total mass of the universe. The WMAP results and constraints imposed by the Big Bang nucleosynthesis of the light elements are inconsistent with much larger amounts of baryonic matter. The gravitational microlensing of stars in the **Large Magellanic Cloud** by **MACHOs (massive compact halo objects)** may demonstrate that some dark baryonic matter is hiding in galactic halos, perhaps in the form of brown dwarfs or stellar-mass black holes. However, a statistical analysis of the microlensing events indicates that only about 19 percent of the mass of the Milky Way’s dark matter halo can be explained by MACHOs.

Dark matter candidates are usually divided into two categories, **hot dark matter (HDM)** and **cold dark matter (CDM)**. Hot dark matter consists of particles moving with relativistic velocities. The leading candidates for hot dark matter are massive neutrinos (which are leptons). Best estimate for the upper limit to the electron neutrino’s mass is  $2.2 \text{ eV}/c^2$ . Cold dark matter candidates

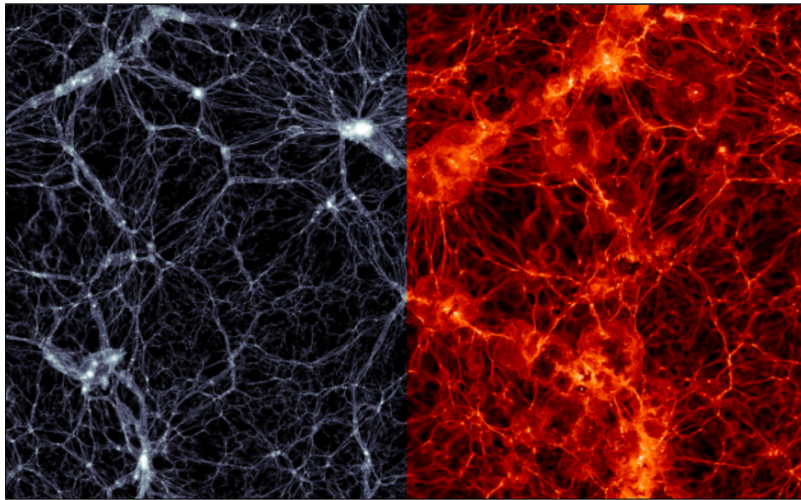


Figure 6.8: Illustris simulation, showing the distribution of Dark Matter

are hypothetical particles that move slowly, such as the WIMPs (weakly interacting massive particles) that hardly interact with normal matter except through their gravitational attraction. It has been suggested that the rest energy of WIMPs may range from 10 GeV (about 10 times more massive than a proton) up to several TeV ( $10^{12}$  eV). Another hypothetical cold dark matter candidate is the axion, a low-mass boson that is extremely lightweight ( $mc^2 \approx 10^{-5}$  eV). If **axions** do exist, and if they constitute most of the dark matter, then they are by far the most numerous type of particle in existence. Although there is as yet no evidence for the existence of WIMPs or axions, the search for them continues.

The distinction between hot and cold dark matter is important because it is difficult for the relativistic hot dark matter to clump together gravitationally and participate in the formation of structure in the early universe. For this reason, models that incorporate cold dark matter are currently favored. In fact, the standard model in cosmology is referred to as the  $\Lambda$ CDM model because it includes both the cosmological constant and cold dark matter.

### The Planck Limits on Time, Mass, and Length

The earliest time that can be addressed by current physical theory is the Planck time. The Planck time is the only combination of fundamental constants that has units of time and, as such, is a characteristic quantity in fundamental theories. It contains Planck's constant, Newton's gravitational constant, and the speed of light, a melding of quantum mechanics, gravitation, and relativity that has yet to be achieved in a unified theory.

**Planck's time:**

$$t_P = \sqrt{hG/c^5} = 5.39 \times 10^{-44} \text{ s}. \quad (6.4)$$

**Planck's mass:**

$$m_P = \sqrt{hc/G} = 2.18 \times 10^{-8} \text{ kg}. \quad (6.5)$$

**Planck's length:**

$$l_P = \sqrt{hG/c^3} = 1.62 \times 10^{-35} \text{ m}. \quad (6.6)$$

The description of the universe before Planck time staggers even the strongest imagination. The universe would have been a collection of primordial black holes that were continually forming,

evaporating, and reforming. In the process, different regions of spacetime were rapidly connecting and disconnecting, giving it a foamlike structure. Our current physical theories break down at times earlier than  $t_P$ , and in fact the very notion of space and time as separate concepts dissolves before Planck time. A quantum theory of gravity capable of describing this convoluted arena in which space and time have lost their familiar, separate identities has yet to be invented. After the Planck time, spacetime began to take on a more coherent structure as greater portions of it became causally connected. Exactly how time itself emerged from the Big Bang is a question to be pondered by physicists and philosophers alike.

### Unification and Spontaneous Symmetry Breaking

It is an article of faith for physicists that before Planck time, the four fundamental forces of nature (the gravitational force, the electromagnetic force, and the strong and weak nuclear forces) were merged into one all-encompassing **Theory of Everything** (TOE). Although the rough outlines of such a theory are still a matter of conjecture, the theory must have certain mathematical symmetries guaranteeing that the four forces were conjoined. When the universe reached the Planck time, the single, all-encompassing TOE force spontaneously separated into the gravitational force (as described by Einstein's theory of general relativity) and a unified version of the three remaining forces. This process is called spontaneous symmetry breaking, a term that refers to the changes in the mathematical symmetries of the theory's equations.

The theories (there are several variants) that describe the joining of the remaining three forces are called **grand unified theories** (GUTs). The simplest GUT, proposed in 1973 by the American physicists Sheldon Glashow and Howard Georgi (both at Harvard), is known as SU(5). The GUTs have had some successes, such as providing a fundamental explanation for the equal magnitudes of the proton and electron charge. They have also had some setbacks; the failure to detect SU(5)'s predicted decay of the proton probably eliminates it as a successful GUT. The moral is that specific predictions based on grand unified theories should be viewed with some caution.

The unification of the strong and weak nuclear forces and the electromagnetic force would have lasted until the temperature of the universe had fallen to about  $10^{29}$  K, when the characteristic thermal energy (kT) of a particle was about  $10^{15}$  GeV and the universe was some  $10^{-36}$  s old. At this point, following another episode of spontaneous symmetry breaking, the strong nuclear force parted company with the electroweak (combined electromagnetic and weak) force.

The theory of the electroweak unification was worked out in the 1960s by three physicists: Sheldon Glashow and Steven Weinberg (American) and Abdus Salam (Pakistani). They described how electromagnetic and weak forces were united when the temperature exceeded about  $2 \times 10^{15}$  K, at roughly  $10^{-11}$  s. At this temperature, the characteristic thermal energy of a particle is about 150 GeV. Their theory predicted the existence of three new particles (the three vector gauge bosons  $W^+$  and  $Z^0$ ) that mediate the weak force, just as photons convey the electromagnetic force. Above kT a few hundred GeV, the vector gauge bosons become massless, and so become indistinguishable from photons. The electromagnetic and weak forces are then unified. When the temperature falls below about  $2 \times 10^{15}$  K, a spontaneous symmetry breaking endows the vector gauge bosons with mass. When these particles were discovered in the 1980s, the agreement between experiment and theory provided a striking confirmation of the electroweak unification. This success provides encouragement to physicists working on GUTs and TOEs.



### Problems with the Standard Theory of the Big Bang

As we move forward from the Planck time, we are confronted by three problems with the simple picture of the Big Bang we have considered so far.

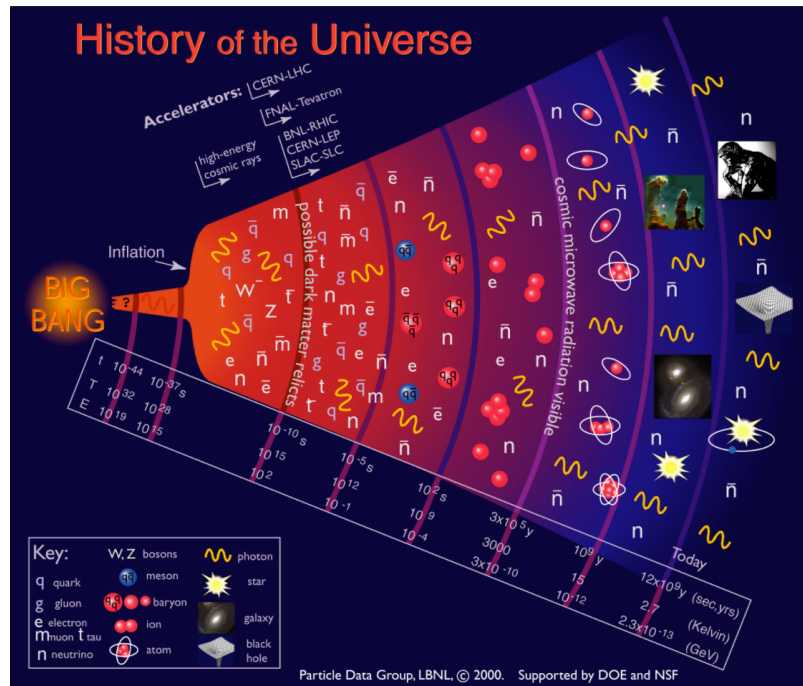


Figure 6.9: Image credits: [Nikhef.nl](http://Nikhef.nl)

**1. Flatness Problem:** A small deviation in the density of the universe causes a lot of difference to the geometry of the universe hence there are some physicists who argue how the universe is so finely tuned.

**2. Horizon Problem:** It says that two points diametrically opposite with respect to us at epoch of CMB were nearly 28 Glyrs apart, but as the age of the universe is only 14 Gyrs how come they are at nearly the same temperature as if in thermal equilibrium. Because information only travels at the speed of light, in order for these distant parts of the universe to communicate with each other, there has to be a faster than light speed transmission of information. In answer to both the above problems **Inflation** has been coined-out, which refers to exponential increase in space-time for a short time during the very early stage of the universe.

**3. Magnetic monopole problem (or Exotic-relics problem):** It says that if the early universe were very hot, a large number of very heavy, stable magnetic monopoles would have been produced. These theories predict a number of heavy, stable particles that have not been observed in nature.

### Inflation

In 1980 an American astronomer working at Stanford University, Alan Guth, proposed a single solution. According to Guth, the Big Bang picture is essentially correct, but during its first fraction of a second, when it was barely greater than zero, the whole universe was much more compact than is described by the standard Big Bang. At that time, every point was close enough to every other point

to be in causal contact, and the entire universe had achieved thermodynamic equilibrium. Then there was a tremendous spurt of **exponential expansion that smoothed out the universe**, rendering it exactly flat.

Guth called this period of exponential growth inflation. This episode of inflation would explain the general isotropy of the universe, and the smoothness of the cosmic background radiation in particular. After inflation, the expansion of the universe proceeded as in the standard Big Bang model.

The details of Guth's inflationary proposal involve ideas at the frontiers of particle physics. In fact, many variants on the original inflationary scenario have been proposed. As observations accumulate, one model may fall out of favor, perhaps to be revived later as more information becomes available. Much research is still ongoing in this area, and the version of inflation described in the following discussion may well be wrong in some of its specifics. However, most cosmologists believe that, because it gives such satisfying answers to so many questions, some form of inflation must have taken place in the early universe.

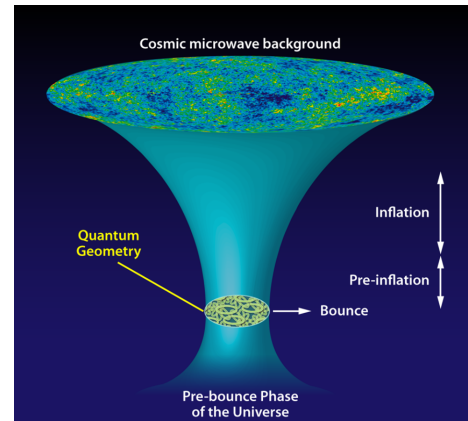


Figure 6.10: Inflation Model

### Virtual Particles and the Energy of the Vacuum

We need not concern ourselves with the highly relativistic particles that were present then. Instead, we will concentrate on another significant component of the very early universe, the energy of the vacuum. The term vacuum requires some explanation. In everyday language, it means a complete emptiness, devoid of any matter or energy. However, physicists use vacuum to describe the ground state of a system.

The existence of the vacuum has been verified by observations of the **Casimir effect** (named for Dutch physicist Hendrick Casimir, 1909–2000). Two uncharged parallel flat conducting plates with a very small separation will alter the properties of the vacuum between the plates. This change in the vacuum creates an attractive force between the plates, which has been measured. Unfortunately, the Casimir effect cannot be used to calculate the value of the energy density of the vacuum.

If we identify dark energy as the energy density of the vacuum, we are faced with a daunting discrepancy of some 120 orders of magnitude between the theoretical and observed values. The huge value calculated for the vacuum energy density is in sharp conflict with the observed rate of the Hubble flow. If every cubic meter were accompanied by approximately  $10^{111}$  J of vacuum energy as the universe expanded and its volume grew, the universe would have expanded so rapidly that no galaxies or stars could ever have coalesced under the influence of gravity.

A plausible physical mechanism for reducing the value calculated for today's vacuum energy density to the observed value of dark energy has yet to be found. According to some advanced particle theories, bosons and fermions should make contributions to the vacuum energy of opposite signs, and so cancel to yield zero vacuum energy. If the cancellation were not perfect, a small observed residual vacuum energy density could result. Why should the cancellation be effective for the first 120 decimal places and then break down? So far the combined efforts of cosmologists and particle physicists have shed little light on this mystery. Nevertheless, we will continue to identify dark energy

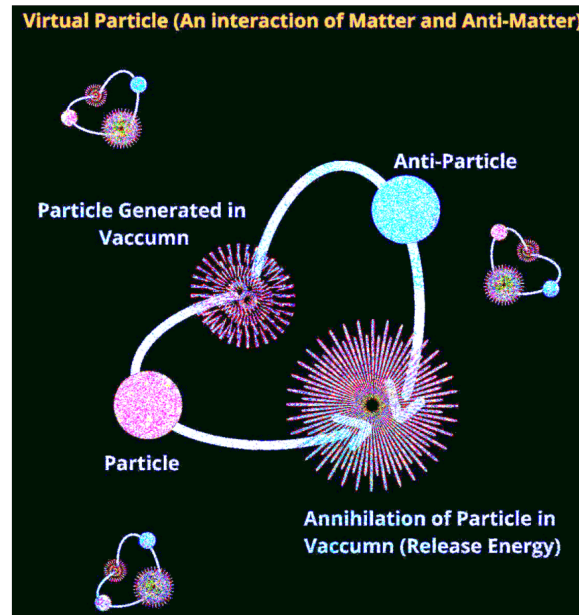


Figure 6.11: Image credits: [Onheaven.co.in](http://Onheaven.co.in)

as the energy density of the vacuum and to accept its presently observed value of nearly zero.

### The False Vacuum

At the end of the GUTs epoch, the universe entered an extremely peculiar state called the false vacuum. The false vacuum that existed when the universe was approximately  $10^{-36}$  s old was not a true vacuum, so the universe was not in the state with the lowest possible energy density. Instead, the universe had entered a supercooled state in which the temperature was suitable for spontaneous symmetry breaking.

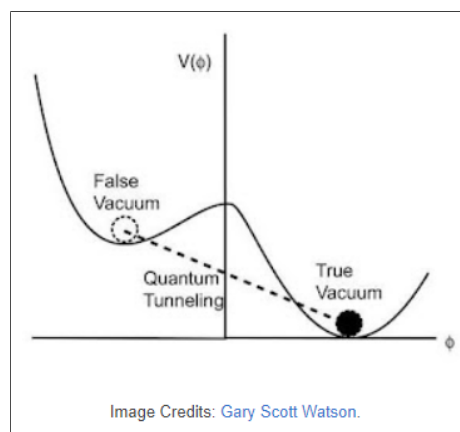


Figure 6.12: Representation of Quantum Tunneling

Supercooling happens when a phase transition proceeds much more slowly than the cooling rate. The universe persisted in its false vacuum state of unbroken symmetry with a high energy

density, even though a spontaneous symmetry breaking to a true vacuum with zero energy density was energetically favorable.

### Quantum Fluctuations and the Onset of Inflation

Inflation began when quantum fluctuations governed by the Heisenberg uncertainty principle which allowed a small region of space to enter a true vacuum state in a universe otherwise filled with false vacuum. Although the pressure within the bubble of true vacuum was essentially zero, it was surrounded outside by the negative pressure of the false vacuum. The greater pressure inside the bubble caused the bubble to grow at an astounding rate.

During this brief time interval, the size of the observable universe grew from  $6 \times 10^{-28}$  m to 0.73 m! There is no reason to believe that the universe conspired to have inflation last exactly long enough to endow only the presently observable universe with a uniform CMB.

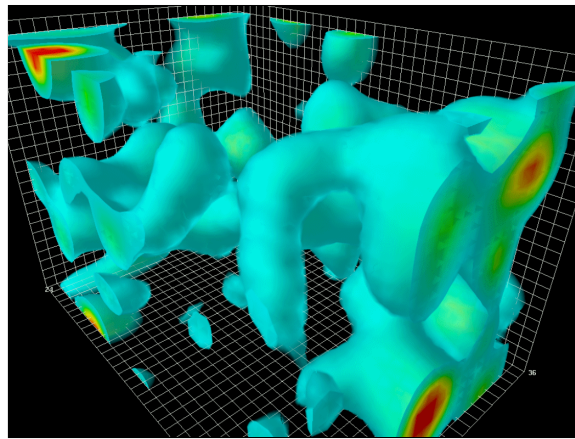


Figure 6.13: To see **3D visualization** of quantum fluctuations of the QCD vacuum [click here](#)

Today's observable universe began inside a small bubble of true vacuum. At the beginning of inflation, every point in the bubble lay within the particle horizon of every other point, and its contents were in thermodynamic equilibrium. The isotropy and homogeneity evident in our universe today were established at that early time. If the size of the presently observable universe immediately after inflation is represented by a hydrogen atom, then the inflated bubble of true vacuum in which it was immersed would be a sphere of radius 200 km!

This episode of inflationary growth came to a halt when spontaneous symmetry breaking finally brought an end to the GUTs epoch, and the strong nuclear force became distinct from the electroweak force. The elevated energy density of the false vacuum was then released, like the release of latent heat that occurs in freezing. This energy reheated the universe to nearly  $10^{28}$  K, its pre-inflation value, and generated a burst of particle–antiparticle creation. From this point onward, the universe developed as previously described in the standard Big Bang picture. But in a single stroke, **this brief instant of inflation resolves the problems with the standard Big Bang.**

### Solutions to the Problems of the Standard Big Bang Theory

The exponential growth of our small bubble of true vacuum carried most of its volume far beyond the boundaries of today's universe. Nevertheless, because the bubble's volume was in thermodynamic equilibrium before inflation, the **spectrum of the CMB is extremely smooth**, thereby solving the horizon problem. The inflation theory predicts that the ultra-fast inflation would have expanded

away any large-scale curvature of the part of the universe we can detect. The **small universe inflated by a large amount and the part of the universe you can observe appears to be nearly flat**. That solves the flatness problem. Inflation allows for magnetic monopoles to exist as long as they were produced prior to the period of inflation. During inflation, the **density of monopoles drops exponentially**, so their abundance drops to undetectable levels which solves the monopole problem.

### Matter–Antimatter Asymmetry

Another challenge cosmologists face is explaining why the universe consists of matter rather than antimatter. All but about 0.01 percent of cosmic rays which sample our Galaxy are matter rather than antimatter.

The explanation of the matter–antimatter asymmetry comes from a combination of the details of grand unified theories and the cooling of an expanding universe following inflation. As we have seen, any particles that were present before inflation would have been diluted to insignificance by the exponential expansion. All of the particles in our universe today originated in the burst of particle–antiparticle production that was fueled by the energy (latent heat) released by the false vacuum. The universe was filled with a soup of quarks, leptons, photons, and even more exotic hypothetical particles simply denoted  $X$  bosons, and their antiparticles  $\bar{X}$ . The spontaneous symmetry breaking that ended the GUTs epoch endowed the  $X$  particles with mass, just as the vector gauge bosons gained mass when the electroweak unification ended. These extremely massive  $X$  particles are not present at the much lower energies that characterize the universe today. According to the grand unified theories, the  $X$  and  $\bar{X}$  particles were present in equal numbers and could be transformed into pairs of quarks and antiquarks and there was a firestorm of particle–antiparticle annihilation that eliminated practically all of the antimatter, leaving only the small excess of baryons that constitutes the visible matter in the universe today. The barrage of photons that was unleashed has since been cooled by the expansion of the universe to become the cosmic background radiation. Nearly all of the photons in the universe are from the CMB; the number produced by other sources (such as stars) pales in comparison.

Because the annihilation of a baryon and an antibaryon produces two photons, this ratio implies that there was roughly one unpaired baryon for every one billion baryon–antibaryon pairs. These unpaired baryons were the tiny residue of matter that survived annihilation to make up the material world.

### The CMB and the Decoupling of Matter and Radiation

CMBR is a **homogeneous** and **omni-directional** glow of microwave radiation. It is also called “**Relic-Radiation**”. You can actually see this ancient light for yourself, when you set a random frequency on an old TV set, some of the random buzz that you see is this ancient ghastly relic from the birth of the universe itself. CMBR actually looks like radiation from a body at a temperature of 2.7K.

The actual story of discovery is quite marvelous and challenged only by the discovery of Hubble’s constant. This starts with Gamow and his coworkers predicting thermal radiation from big bang remains. The calculation being further improved by Dicke and Peebles estimating it to be a black-body radiation of about 5 K. As a result, they started to make an antenna to detect this radiation however they were scooped by two Bell Labs scientist, Arno Penzias and Robert Wilson who had a found out an excess of 4.2 K antenna temperature which was isotropic and not of terrestrial, solar or galactic origin. When these two results were combined these two facts were known.

1. The radiation had indeed a thermal origin of nearly 3K.

2. The radiation was isotropic with a primary fluctuation due to motion of Earth around Sun and that of Sun in Milky Way Galaxy which once removed the radiation is very nearly isotropic with the only fluctuations expected from Quantum fluctuations in a very nearly uniform gas. If there would have been some observer this is what the early universe would have looked like very bright.

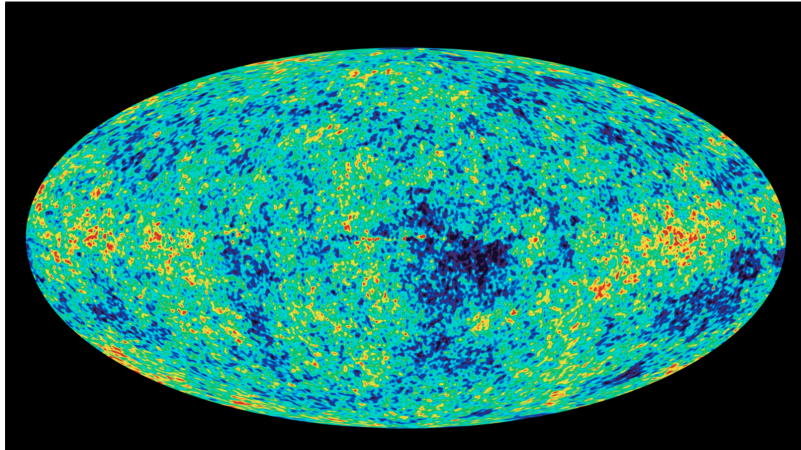


Figure 6.14: Cosmic Microwave Background(CMB)

The resulting drop in the opacity decoupled the radiation from the matter in the universe and allowed the photons to roam freely. This decoupling had dramatic implications for the collapse of higher-density regions and the subsequent formation of structure in the universe.

### 6.2.2 Origin of Structure

Even a momentary glimpse at the night sky provides convincing evidence that the universe is not perfectly homogeneous. Structure abounds on all scales, from planets to superclusters of galaxies.

#### Determining When the First Stars and Galaxies Formed

A galaxy discovered far beyond the galactic cluster Abell 2218 illustrates just how tight the timing for galaxy formation is. This corresponds to a time just 780 million years after the Big Bang, just 5.7 percent of the present age of the universe. The galaxy is tiny, perhaps just 600 pc in diameter. Nevertheless, it is a site of extremely active star formation. It is fortunate that Abell 2218 served as a gravitational lens that magnified the image of this farthest galaxy and allowed it to be detected. The presence of such a young galaxy serves as a severe constraint on theories of structure formation. Because it formed less than 1 billion years after the Big Bang, it must have formed extremely rapidly (perhaps by the process of dissipative collapse discussed). One clue pointing to the time when the first stars and galaxies were formed comes from observations of the Lyman- $\alpha$  forest in high- $z$  quasars. The closely spaced Ly- $\alpha$  absorption lines are produced by clouds of neutral hydrogen of smaller redshift that lie between the quasar and Earth. Neutral hydrogen is a very efficient absorber of 122-nm (UV) photons. However, if, after recombination at  $z = 1089$ , all of the hydrogen in the intergalactic medium remained neutral, then almost all of the Ly- $\alpha$  forest should be reduced to zero due to absorption by the intergalactic neutral hydrogen. In effect, the neutral hydrogen in the intergalactic medium would act as an absorbing cloud with a continually declining redshift in the direction of Earth. This indicates that the hydrogen in the intergalactic medium is not neutral but almost completely ionized. We conclude that after recombination, the universe entered a

“**Dark Age**”, before the first stars and galaxies had formed and started to shine. Then UV radiation from the first generation of stars and AGN reionized the universe, and it has remained ionized until the present time. If we can find a flattening of the Ly forest for a high- $z$  quasar, then we know that we are observing that quasar during the **epoch of reionization**. This flat region in a quasar’s spectrum is called the **Gunn–Peterson trough**, named for the astronomers who predicted it, James Gunn (American) and Bruce Peterson (Australian). The relatively rapid diminishing of the Ly $\alpha$  forest indicates that the reionization of the intergalactic neutral hydrogen was finished by  $z = 6$  and that its final stages occurred very quickly. We may very well be penetrating back to the end of the “Dark Age.”

According to the WMAP results, the first stars ignited about 200 million years after the Big Bang. The Spitzer Space Telescope may have detected the light (shifted to infrared wavelengths) from the first generation of objects that initiated the reionization of the universe. Following a deep, 10-hour exposure in the direction of the constellation Draco, all known objects were carefully subtracted from the image. An infrared background remained, with blobs that may be the glow from the very first stars (Population III).

### Top-Down Galaxy Formation and Hot Dark Matter

As noted previously, it is intriguing that the two mass values to emerge from recombination roughly span the mass range of galactic structure. The Jeans mass is typical of a globular cluster of stars. In addition, the lower limit for the mass of adiabatic fluctuations that survived the acoustic oscillation phase before recombination, is characteristic of an elliptical cD galaxy or a small cluster of galaxies. (Adiabatic density fluctuations and hot dark matter are thought to behave similarly, because they both tend to resist clumping through the diffusion of photons and fast-moving particles.) The resulting top-down process of galaxy formation involves the breakup of larger structures. The problem with this process is that the breakup may occur too late to be consistent with the observed times of formation of the earliest galaxies. Any clumping that occurs involves large amounts of mass (representative of galactic clusters and superclusters) and so must be involved in a top-down process for forming galaxies from the breakup of larger entities.

### Bottom-Up Galaxy Formation and Cold Dark Matter

On the other hand, cold dark matter is slow moving and should accumulate much more easily. Concentrations of cold dark matter can begin to collect on a variety of mass scales when the matter era begins, resulting in a bottom-up scenario for forming galaxies from the assembly of smaller components. The difficulty with the cold dark matter model is that numerical simulations of the early universe have trouble reproducing the galactic voids found in redshift surveys. It has been found if galaxy formation is biased, so galaxies tend to form more readily in overdense regions, this problem with cold dark matter can be overcome. Current observations and interpretations strongly favor a bottom-up process for the formation of galaxies. The bright galaxies we observe today were assembled from fragments at high redshift.

### An Interesting Question

#### “Why are we here?”

The answer is amazing : We are here because, 13.7 billion years ago, the universe borrowed energy from the vacuum to create vast amounts of matter and antimatter in nearly equal numbers. Most of it annihilated and filled the universe with photons. Less than one part per billion survived to form protons and neutrons and then the hydrogen and helium that make up most of everything there is. Some of this hydrogen and helium collapsed to make the first generation of massive stars,

which produced the first batch of heavy elements in their central nuclear fires. These stars exploded and enriched the interstellar clouds that would form the next generation of stars. Finally, about 4.6 billion years ago, one particular cloud in one particular galaxy collapsed to form our Sun and its planetary system. Life arose on the third planet, based on the hydrogen, carbon, nitrogen, oxygen, and other elements found in the protostellar cloud. The development of life transformed Earth's atmosphere and allowed life to move onto land.



Figure 6.15: Image credits: *HdWallpaperim*

Sixty-five million years ago, a fortunate collision with a large meteoroid hastened the demise of the dinosaurs and allowed small, furry mammals to take center stage. Primitive men and women evolved and moved out of Africa to conquer the world with their new knowledge of tools, language, and agriculture. After raising food on the land, your ancestors, your parents, and then you consumed this food and breathed the air. Your own body is a collection of the atoms that were created billions of years earlier in the interiors of stars, the fraction of a fraction of a percent of normal matter that escaped annihilation in the first microsecond of the universe. Your life and everything in the world around you is intimately tied to countless aspects of modern astrophysics.

### 6.2.3 **References:**

1. *Elementary particles*
2. *Dark Matter*
3. *GUTs: The Unification of Forces*
4. *Big Bang Theory*
5. *A Glance at the Earliest Universe*
6. *Virtual Particle*
7. *Quantum Fluctuation*
8. *Cosmic microwave background*





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